LECTURE NOTES ON FLUID MECHANICS

4TH SEMESTER MECHANICAL ENGINEERING

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TH-3 FLUID MECHANICS

Name of the Course: Diploma in Mech & Other Mechanical Allied Branches					
Course code: Semester 4 th		4 th			
Total Period:	60	Examination	3 hrs		
Theory periods:	4 P/W	Class Test:	20		
Maximum marks:	100	End Semester Examination:	80		

A. RATIONAL:

Use of fluid in engineering field is of great importance. It is therefore necessary to study the physical properties and characteristics of fluids which have very important application in mechanical and automobile engineering.

B. COURSE OBJECTIVES:

Students will develop an ability towards

- Comprehending fluid properties and their measurements
- Realizing conditions for floatation
- Applying Bernoulli's theorem

C. TOPIC WISE DISTRIBUTION OF PERIODS

<u>Sl. No.</u>	<u>Topic</u>	<u>Periods</u>
01	Properties of Fluid	08
02	Fluid Pressure and its measurements	08
03	Hydrostatics	08
04	Kinematics of Flow	08
05	orifices, notches & weirs	08
06	Flow through pipe	10
07	Impact of jets	10
	Total Period:	60

D.CONTENT

Properties of Fluid

Define fluid

Description of fluid properties like Density, Specific weight, specific gravity, specific volume and solve simple problems.

Definitions and Units of Dynamic viscosity, kinematic viscosity,

surface tension Capillary phenomenon

Fluid Pressure and its measurements

Definitions and units of fluid pressure, pressure intensity and pressure head.

Statement of Pascal's Law.

Concept of atmospheric pressure, gauge pressure, vacuum pressure and absolute pressure

Pressure measuring instruments

Manometers (Simple and Differential)

Bourdon tube pressure gauge(Simple Numerical)

Solve simple problems on Manometer.

Hydrostatics

Definition of hydrostatic pressure

Total pressure and centre of pressure on

immersed bodies(Horizontal and Vertical Bodies)

Solve Simple problems.

Archimedes 'principle, concept of buoyancy, meta center and meta centric height (Definition only)

Concept of floatation

Kinematics of Flow

Types of fluid flow

Continuity equation(Statement and proof for one dimensional flow)

Bernoulli's theorem(Statement and proof)

Applications and limitations of Bernoulli's theorem (Venturimeter, pitot tube)

Solve simple problems

Orifices, notches & weirs

Define orifice

Flow through orifice

Orifices coefficient & the relation between the orifice coefficients

Classifications of notches & weirs

Discharge over a rectangular notch or weir

Discharge over a triangular notch or weir

Simple problems on above

Flow through pipe

Definition of pipe.

Loss of energy in pipes.

Head loss due to friction: Darcy's and Chezy's formula (Expression only)

Solve Problems using Darcy's and Chezy's formula.

Hydraulic gradient and total gradient line

Impact of jets

Impact of jet on fixed and moving vertical flat plates

Derivation of work done on series of vanes and condition for maximum efficiency.

Impact of jet on moving curved vanes, illustration using velocity triangles, derivation of work done, efficiency.

CHAPTERS COVERED UP TO IA-1, 2,3,4

Learning Resources:

Sl No.	Name of the Book	Author Name	Publisher
1.	Text Book of Fluid Mechanics	R.K.Bansal	Laxmi
2.	Text Book of Fluid Mechanics	R.S khurmi	S.Chand
3.	Text Book of Fluid Mechanics	R.K.Rajput	S.Chand
4.	Text Book of Fluid Mechanics	Modi & Seth	Rajson's pub. Pvt. lt

** HLUID ** MECHANICS

PROPERTIES OF FLUTOS:

(1) Density on Mass Dunsity :-

of Density or man density of a fluid is defined as the matio of the mass of a fluid to its volume. Thus mass per unit volume of a blush is called density. It is denoted by the symbol of (the). The unit of mass density in S.I. unit is kg per cubic metae tie. Kg/m3,.

- The density of liquids may be considered as constant while that of gases changes with the vanilation of pressure and temperature.

- Mathematically, moss density is written as f = Mais of bluid = m Volume of bluid = V

-7 The value of density of water to 1gm/cm3 or 1000 kg/m3.

(R) Specific Weight on Weight Density:

TSpecific weight on weight Density of a fluid is the natio between the weight of a bluid to its volume. Thus weight per unst volume of a fluid is called weight density and it is denoted by the symbol W.

Thus mothernatically, w= weight of bluid

Here, weight of third = mass of blund × Acceleration due to

=) Weight Density (w)= mg = mass of bluid xg

= dxg

+ The unit of weight density in S.I unit is Newton / m3.

The value of specific weight on weight density (w) for water is 9-81 × 1000 Newton Im3 in S.I. units.

[3] Specific Volume:

Specific volume the a Muid is defined as the volume of a Huid is occupied by a unit mass on volume per unit mass of a Huid is called Specific volume. Mathematically , it is expressed as Specific volume = Volume of Huid

Specific Volume = Mays of bluid = 1

Mays of bluid = 7

volume of bluid

7 Thus specific volume is the necephrocal of mass density.
7 It is expressed as m3/kg.
7 94 is commonly applied to gases.

Specific gravity is defined as the notio of the weight density (on density) of a standard density of a standard density of a standard thuid. For liquids, the standard thuid is taken water and for gases, the standard thuid is taken water and for gases, the standard thuid is taken water and for gases, the standard thuid is taken water and for gases, the standard thuid is taken our. Specific growty is also called relative density. It is dimensionless quantity and is denoted by the symbol S.

Modhematically, S(box liquids) = weight density but liquid toeight density of water

es (born gases) = weight density of your

Thus weight density of a liquid = S x weight density of water = SX1000 x 9.81 N/m3

The density of a liquid = Sx Density of winder = SX 1000 kg/m²

Density of Standard liquid =
$$\frac{feg}{fwg} = \frac{fe}{fw}$$

=> $\frac{fl}{fw} = \frac{fl}{fw}$
=> $\frac{fl}{fl} = S \times fw$

96 the specific greatly of bluid is known, then the density of the bluid will be aqual to specific greavity of bluid multiplied by the density of water . For example, the specific gravity of mercury To 13.6, Hence density of marcuny = 13.6 x 1000 3 S Hg

-: VISCOSITY :-

-7 Viscocity is defined as the property of a bluid which oftens resistance to the movement of one layer of bludd over another adjacent layer of the fluid.

+ When two layers of a bluid, a distance by aparet, move one over the other at different velocities, say u and utdu as shown in bigune, the Viscocity together with relative velocity Causes a shear stress acting between the bluid layous.

-17 The top layer causes a shear stress on the adjacent lower layer while the lover layer courses a shear street on the adjacent top layer. The shear Stress is proportional to the mate of change of velocity with respect to y. It is denoted by symbol (Volonia in The

(Velocity Vointation Wear a solid boundary)

Velocity

C (Tow). Malhomotically. To dy of T= 12 dy

the where it is the constant of proportionality and is known as the constitution of dynamic Visionity are only Visionity,

du represents the rode of shear strain on rode of shear deformation on velocity quadient.

from equal we have, to = (du)

Thus Viscosity it also defined as the shear stress required to Produce unit reade of Shear Stream

$$\mu = \frac{\text{force}}{\text{Area}} + \frac{\text{d}u}{\text{obs}}$$

$$= \frac{N/m^2 \times \text{d}y}{\text{obs}} = \frac{N}{m^2} \times \frac{m}{m/s} = \frac{N_s c}{m^2}$$

SI unit of Viscosity = NS/m2 = pars. = Newton-sea

Acceleration = Speed Sec

then, $\mu = \frac{N.s}{m^2}$ => \mu = \frac{kq \frac{m}{s} \chi \chi \s}{s^2} \chi \s
== \frac{kq \frac{m}{s} \chi \chi \s}{m^2}

(Newton = mass xacceleration)

The unit of viscosity in class is also called poise which is equal to dine-see.

The numeral col conversion of the unit of Viscosity broom 1965 wish to cops unit is given below.

But 1 Newton = one kg (mass) & one To [acceleration] = 1000 gm x 100 (m = 1000 x 100 gm-cm sort-= 1000 xloo dyne one kgt sec = 9.81 x locopo dyne-sec = 7.81 XLOUDO Ayre-cec broxtoox cm2 = appl 98-1 dyne-lec = 98-1 poise Thus box solving numerical problems, it viscocity is given in posses, it must be divided by as-1 to get its equivalent value in Mks. one kyb-sec = 9-81 NS = 98-1 poise one NS = 98.1 poise = 10 poise 7 1 poise = 10 NS 7 1 poise = 10 NS Det is defined on the rection between the dynamic viscosity KINEMATIC VISCOSITY 7 and density of bluid. Set is denoted by Greek symbol (V) called inu. Thus mathematically, V = Viscosity = 12 The units of kinematic Viscocity is obtained as V = units of \$ = force x Time = force x Time.

Voits of P (Length) x (Length) Length - Mass x length x Time

(Time) 3 x Time

(Mass)

(Length) 2 S. Fonce = Mass x Acc

- Mass x Length

Those Time? In take and si, the unit of Kinematic hiscosity is Imetrical/sec one majore whole in Cops units it is whitten as cm2/s.

In CGS units, Kinematic Macrosomy is delso known as stroke. Thus, one stroke = $cm^2/s = (\frac{1}{100})^2 \, m^2/s = 10^{-4} \, m^2/s$. Centulake means = $\frac{1}{100} \, stoke$

SURFACE TENSION AND CAPILLARITY 7

Surface Tension is defined as the tensile force acting on the surface of a liquid in contact with a gas one on the surface between two immissible lequids such that the contact surface between two immissible lequids such that the contact sunface behaves loke a membrane under tension. The magnitude of this force per unit length of the free surface magnitude of this force per unit length of the free surface will have the same value as the surface energy per unit ones of its denoted by Graek *letter & (routed sigma). In Mks units, it is expressed as kgt/n while in st units as N/m.

SURFACE TENSION ON LIQUID DROPLET ?

Consider a small spherical droplet of a liquid of readous n. On the entire surface of the droplet, the tensile borce due to surface tension will be acting.

Let of surface tention of the liquid

pressure intentity incide the dropplet (in excess

of the outside pressure intentity)

d= Dia of droplet

Let the droplet is cut into two halves. The forces acting to

one half (say left half) will be

(9) Tensite fonce due to Surface tension acting anound the encumberrance of the ocut pontion as shown in figure. and this is equal to = TX concumpanence = TXRd

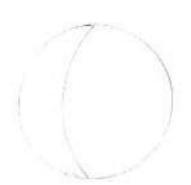
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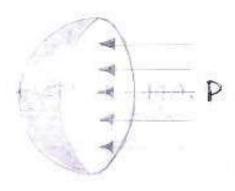
(11) Pressure borece on the area of d2 = PX To d2 as shown in figure. These two borces will be equal and opposite under equilibratum conditions. The.

$$P = \frac{G \times \pi d}{\pi \times d^2} = G \times \pi d$$

$$P = \frac{G \times \pi d}{\pi \times d^2} = \frac{46}{d} \longrightarrow \frac{1}{2}$$

The above equation shows that with the decrease of diameter of the droplet, pressure intensity inside the droplet increases.





(0) Droplet

(B) Sunface (FORCES ON DROPLET

(C) PRESSURE FORLLES

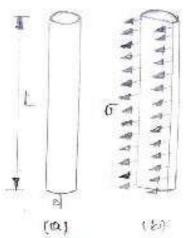
SURFACE TENSION ON A LIQUID JET =

Consider a lequid set of diameter of and tength "L" as shown in Figure.

Let p= pressure intensity inside the liquid Jet above the outside Pressure

U = Surface tension of the liquid Consider the equilibrium of the Semi set, we have force due to Pressure - px ranea of semi set = PX LXd

torce due to surface tension = 0x2L



FIREES ON LIQUID

Equating the forces, we have $p \times L \times d = \sigma \times 2L$ $\Rightarrow P = \frac{G \times 2L}{L \times d}$

SURFACE TENSION ON A HOLLOW BUBBLE of A Hollow bubble like a some bubble in air has two surfaces in contact with air, one inside and other outside. Thus two surfaces are subjected to surface tension. In such case, we have

- CAPILLARITY :-

or Capillarity is defined out a phenomenon of the orthogen of liquid when the tube is held vertically in the liquid. The tise of liquid surface is known as Capillary tise while the ball of the liquid surface is known as Capillary tise while the ball of the liquid surface is known as Capillary degrees.

of It is expressed interms of Cm on mm of liquid. Its value defends upon the specific weight of the liquid, diameter of the tube and sunface tension of the liquid.

Expression for Capillary Rise:

Consider a glass tube of small diameter of opened out both ends and is insented in a liquid, say water. The liquid will rise in the tube above the level of the liquid.

Let he height of the liquid in the tube. Under a state of aquilibrium, the weight of liquid of height his balanced by the force of the surface of the liquid in the tube. But the force at the surface of the liquid in the tube is the tube to surface of the liquid in the tube is the

Let G = surface tension of liquid 0 = Angle of Contact between liquid and glass tube The weight of liquid of height h in the tube = (Arrea of tube xh) = #d3xhxpxg - 1 (CAPILLARY RISE) when P = Density of liquid Vertical component of the surface tensile force = (X circumberence) X cos B = TX nd x cos 0 For equilibrium, equating (1) & (2), we get The dah por = TXTE x cos on The TARDX COS B = 40 COS B - 3

The value of 0 between water and clean glass tube is approximately equal to zero and hence cos a is equal to unity. Then rise of water is given by

h= 45 - 9

Expression for Capillary Fall:—

Et the glass tube is dipped in mercury, the level of mercury in the tube will be lower than the general level of the Cutside Inquid as shown in the figure.

Ket Mattelght of depression in tube

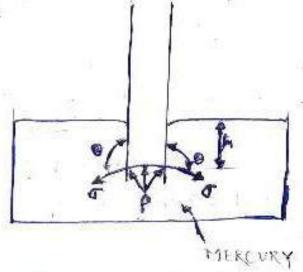
Then in equilibrium, two forces one acting on the mercury inside the tube. First one is due to surface tension acting in the downward direction and is equal to FX tol x cos a.

Second boace is due to hydrostatic boace acting upward and is equal to intensity of pressure at a depth h'x Arrea

= PX \(\frac{1}{4} a^2 = pg xhx \frac{11}{4} a^2 \)
(" P= Pgh)

Equating the two, we get $G \times \pi d \times \cos \theta = \rho g h \times \frac{\pi}{4} d^2$ $\Rightarrow h = \frac{46 \cos \theta}{\rho g d}$

.. Value of 0 for mercury, and glass tube is 1280.



(CAPILLARY FALL)

Consider a small Area of in large mass of bluid. It the bluid is stedionary then the force exerted by the surrounding bluid on the area of will always be perpendicular to the surface of .

Let of is the force earling on the area of in the normal direction. Then the matio of $\frac{dF}{dA}$ is known as the intensity of Pressure on Simply pressure and this reation is represented by P. Hence mathematically the pressure at a point in a bluid at rest is $p = \frac{dF}{dA}$

It the Fonce (F) is uniborary distributed over the Area (A), then pressure at any point is given by

P= F = Porte Arcea

: Force or pressure force, F= PXA.

The unit of pressure are it kgt/m² and kgt/cm² in MKS unit.

(ii) Newton/m² on N/m² and N/mm² in II unit.

N/m² is known as pascal and is represented by Pa.

other Commonly used units of pressure are:
kpa = kilo pascal = 1000 N/m2.

bar = 100 kpa = 105 N/m2.

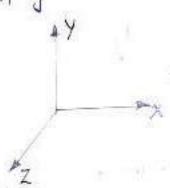
PASCAL'S LAW >

It states that the pressure on intensity of pressure at a point in a static fluid is equal in all directions.

This is proved at!

The fluid element is of very small dimensions.

ie da, dy and ds.



Px.oly.1 da da c

(FORCES ON A FLUID ELEMENT

Consider an arbitrary bluid element of wedge shape in a bluid mans at nest as shown in bigure. Let the width of the bluid mans at nest as shown in bigure. Let the width of the element pierpendicular to the plane of paper is unity and pa, by and Pz are the pressures on intensity of pressure acting on the face AB, AC and BC respectively. &

Let LABC = 0, then the bornces acting on the element are:

(1) Pressure forces normal to the suntaces and

(3) Weight of element in the ventical direction.

The forces on the faces one :-

Force on the bace AB = PXX AREA of bace AB = PXXAYX1

Similarly force on the bace AC = Pyxdx X I

borce on the bace BC = Pz xds X 1

weight of element = (Mais of element) x g

= (Volume x p) x g

= (AB x AC x 1) x p x g

where P= olensity of bluid

Resolving the borces in x-direction, we ha

Px Xdy X1 - Pzds X1 cos D = 0

on But from bigune, ols coso = AB = dy

Px xdy xL - Pzxdy x1 = 0

Px = Pz

on similarly, resolving the borces in y-direction, we get

by xdxx1-px xds x Less (90-0) - dxxdy x1 x f xg=0

y pydx + pzds sin 0 - dxdy x f xg = D

1 DR/. Let the width of the elements is 1 Hence

the area of bonce on face AB = dy x 1 (FAB = Pyxdyxi)

area of bonce on face AC = dx x1 (FAC = Pxxdxxi)

area of bonce on face BC = dx x1 (FBC = Pxxdxxi)

Weight of element = (mase of element) x g
= f x values x g
= f x (\frac{1}{2} AC x AB x 1) x g

For equilibraium

Considering the body at equilibraium

Resolving the left and right borces.

FAS = FBC COS O -> Py. dy. 1 = Px ds 1 cos 0 => py, dy = Pz, do tos os + cos 10 = MB x dy -> ds cos o = dy

Applying this in the expection Py.dy = Pz.dy

wpy = Pz - 0

Resolving the up boreses and down boreses FAC = FBC, Six 0 + 10

> => Px dx -1 = Pz ds 1. sins + fx(2-dx; dy 1) x g of Pada = Pads sir 0 + fg dady

as da, dy will be very small, Hence I can be neglected. Applying in the equation

Pa, da = Pz da => Px=Pz

: Px=Pn=Pz - 0

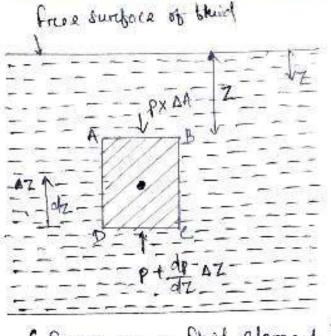
PRESSURE HEAD & HYDROSTATIC LAW :+

The pressure out any point in a bluid at rest is obtained by the Hydrostatic Law which states that the rate of increase of pressure in a ventical observant direction must be equal to the weight density of the blund out the points

Let AA = Cross Sectional Acea AZ = Height of bluid element

P = pressure on face AB

Z= Distance of bluid element from bree surface W = weight density of bluid



(Forces on a fluid element)

for equilibrium

$$D + (P \times \Delta A) = (P + \frac{dP}{dz} \Delta Z) \Delta A$$

$$\Rightarrow [P(\Delta A + \Delta Z)g] + P \times \Delta A = (P + \frac{dP}{dz}) \Delta Z \cdot \Delta A$$

$$\Rightarrow P \cdot \Delta A \cdot \Delta Zg + P \cdot \Delta A = P \cdot \Delta A + \frac{dP}{dz} \cdot \Delta Z \cdot \Delta A$$

$$\Rightarrow P \cdot \Delta A \cdot \Delta Zg = \frac{dP}{dz} \cdot \Delta Z \cdot \Delta A$$

$$\Rightarrow P \cdot \Delta A \cdot \Delta Zg = \frac{dP}{dz} \cdot \Delta Z \cdot \Delta A$$

$$\Rightarrow P \cdot \Delta A \cdot \Delta Zg = \frac{dP}{dz} \cdot \Delta Z \cdot \Delta A$$

This equation is known as Hydrostatic Law.

$$\frac{d\rho}{dz} = fg$$

$$\Rightarrow \int d\rho = \int fg dz \qquad \left(\begin{array}{c} \cdot \cdot \cdot Z = \frac{P}{fg} \end{array} \right)$$

$$\Rightarrow P = fgZ$$

4

TYPES OF PRESSURES !-

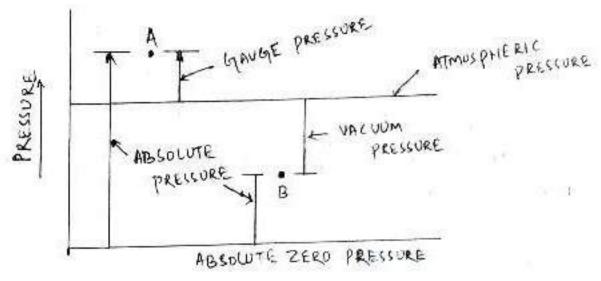
- The pressure on a build is measured in two different systems. In one system, it is measured above the absolute Zerro on Complete, Vacuum and it is called the absolute pressure and in other system pressure is measured above the atmospheric pressure and it is called gauge pressure. There are different types of pressure in the system.
 - @ Absolute pressure
 - 3 Gauge Pressure
 - 3 Vacuum pressure
 - (2) Absolute Pressure of the pressure which is measured with the help of a pre- reference to eubsolute Vacuum pressure.
 - (3) Engage Pressure =>

 It is defined as the pressure which is measured with the help of a pressure measuring instrument, in which the atmospheric pressure is taken as cladum. The atmospheric pressure on the scale is marked as Zerro.
- (3) Vacuum pressure =>
 To is defined as the pressure below the atmospheric
 Pressure.
 - The relationship between the absolute pressure gauge.

 Pressure and vacuum pressure are shown in figure bolow.

 Mathematically.
 - (i) Absolute pressure & Gauge pressure + Atmospheric pressure on Pab = Patry & Pagage

(fi) Vacuum Pressure - Atmospheris pressure - Absolute pressure - 7 Pval = Palm - Pab



[Relationship between Pressures]

MEASUREMENT OF PRESSURE 9

The pressure of a bluid is measured by the following devices:

1. Manometers 2. Mechanical Gauges

(1) MAHOMETERS 7

Manometers are defined as the devices used box measuring the pressure at a point in a blud by balancing the column of built by the same on another column of the bluid. They are classified as:

(a) simple manamedens

(b) Differential Manomelers

(2) MECHANICAL GAUGES 9

the pressure by belancing the build column by the spring or dead weight. The commonly used mechanical pressure gauges are:

(a) Diaphragm Pressure gauge (c) Dend-weight pressure gauge
(b) Boundon tube pressure gauge (d) Bellows Pressure gauge

1 calculate the dencity, specific weight and weight of

m = 3 m = 3

V= 1 lil = 10-3 m3/103 (m3 S = 0.7

S = whoy = for y

\$S = floq looky |m3

7 0.7 = floor kg/m3

3 -f lig = 65000 7 × 1000 = 700

W= fxg = 700 x 9.81 = 6867 N/m3

W=mg = fx xxg

= 700 XVX9.8 = 700 X 10-3 X9.81

W = 6867 X 10-3 = 6.867 N

(Ans)

Q.3 Two horizontal plate care place 1.25 (m apart from each other 2 the space between them is filled with oil of viscosity 14 poise. Calculate the shear stress in oil & it the upper plate is moving with a velocity of 2.5 mgs.

 $M = 1.25 \text{ cm} = 1.25 \times 10^{-2} \text{ m}$ $N = 14 \text{ poise} = 14/10 = 1.4 \text{ N/m}^2$ $V_2 = 2.5 \text{ m/s}$

91=D

13 Find the kinematic Viscocity & specific greatly of an oil having density of 98t kg/m3. The shear stress out a point in oil is 02452 N/m2 & velocity gradient is given by 0.2/sec.

(My)
$$f = 981 \text{ kg/m}^3$$
 $7 = 0.2452 \text{ N/m}^2$
 $5 = 7$
 $\frac{du}{dy} = 0.2/sec$
 $\frac{du}{dy} = \frac{1226 \text{ NS/m}^2}{1000}$
 $\frac{du}{dy} = \frac{1226 \text{ NS/m}^2}{1000}$

Get The relocity distribution from flow over a floot plate is given by U=3/4y-y2 in which U is the velocity in m/s 2 y is the distance in metre above the plate Determine the shear stress at y=1.5 m & the dynamic viscosity at 8.6 poise

\$ ch of y =1.5 m

then,
$$\frac{du}{dy} = \frac{3}{4} - \frac{3}{4} = \frac{3}{4} = \frac{3}{4} = \frac{-9}{4} = -2.25$$

: SIMPLE MANDOMETERS

A simple manometer consists of a glass tube having one of its ends connected to a point where pressure is to be measured and other end remains open to admosphere. Common types of simple manometers are:

(1) piezometer .

(3) U-tube manometers and

(3) Single Column manometer.

4) PLEZOMETER >

Det is the simplest from of manometer used bor measuring gauge pressures. One end of this manometer is connected to the point where pressure is to be measured and other end is open to the

almosphere as shown in bigune,

Bressure head at that point.

It dot a point A, the height of liquid

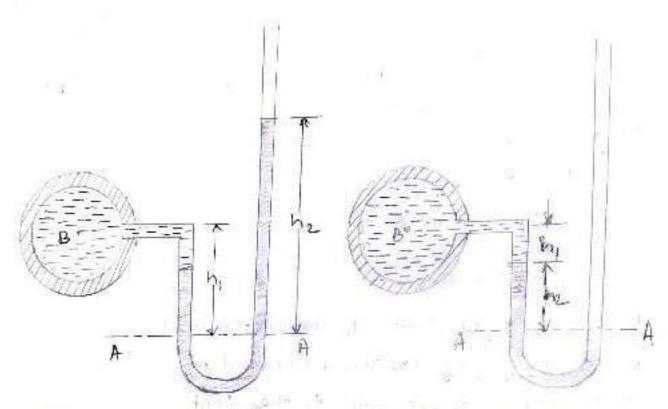
say who water is h in presometer tube, then pressure at $A = \frac{1}{10} \times 9 \times h \frac{10}{m^2}$

Prezo meder

(2) U-TUBE MANOMETER =>

It consists of glass tube bent in U-shape, one end of which is connected to a point at which possessure is to be measured, and other end remains open to the atmosphere as shown in & the bigure. The tube generally contains mercurey ore any other liquid whose specific gravity is greater than the specific gravity

Of the liquid whose pressure is to be measured.



(a) For Gauge pressure

(b) For Vacuum pressure

(A) FOR GAUGE PRESSURE =>

Let B is the point out which pressure is to be measured, whose value is p, the dadum line is A-A.

Let his height of Right liquid outsove the doctum line

haz height of theavy liquid above the datum line

SI = Specific growty of layout liquid

fit Darsity of light liquid = 1000 x Si.

Sz = Specific growny of heavy liquid

P = Denuty of heavy liquid = 1000 XS2

As the pressure is the same for the horizontal surface, Here pressure above the horizontal doctum line A-A in the left court and in the right column of V-tube manameters. Should be sime

Pressure above A-A in the right column = P+P+xgxh,
Pressure above A-A in the right column = P2×gxh2

Hence repeating the two pressures. p+pigh = fighz > P= P29h2-Pi3h1 - (1)

(B) FOR VACUUM PRESSURE => For measuring vacuum pressure, the level of the heavy liquid in the manometer will be as shown in the above briguize. Then pressure above 4-4 in the left column = fight Pightp pressure head in the right column above A-A = 0 1. Hence Paghet Pighi+P=D 7 P=- (2)

[3] SINGLE COLUMN MANOMETER =>

Single Column manameter is a modified from of a U-tube manometers in which a reservior thowing a large cross-sectional area (about 100 times) as compared to the area of the tube is Connected to one of the limbs (say left (mb) of the manometer as shown on bigune. Due to large exist-sectional area of the reservoor, bor any variation in pressure, the change in the liquid level in the reservaire will be very small which maybe neglected and thence the pressure is given by the height of liquid in the other limb. The other limb may be vertical on inclined. Thus there are two types of single column manometer as; (1) Vertical single column marximeters

(2) Inclined single column manometers

(1) VERTICAL SINGLE COLUMN MANDMETER ?

The bigure shows the ventical engle column manometer.

Let X-X be the datum line in the reservoire and in the reight line of the manometer, when it is not connected to the pipe, when the manometer is connected to the pipe, when the manometer is connected to the pipe, due to high pressure out A, the heavy loqued in the reservoire will be pushed downward and will risk in the reight limb.

Let Ih = fall of heavy liqued in

hz = Rise of heavy liquid in right limb hi = Height of Centre of Pipe 7 oubove X-X

PA=Pressure at A, which is to be measured

A - Cross. sectional Area of

a = Creats_sectional area of the reight lamb

Si = Sp. gravity of liquid in pipe

Sz = Sp. grawty of heavy liquid in reservoir and right Himbs

Pr = Dansity of legical in pape

fz = Denaty of toquid in nesenvoin

Fall of heavy liquid in reservior will course a ruse of heavy liquid

 $A \times \Delta h = \alpha \times h_2$ $\Rightarrow \Delta h = \frac{\alpha \times h_2}{A} \qquad (0)$

Now consider the doctum line Y-Y as shown in biquie, then pressure in the reight timb above Y-Y.

= f2 x gx (bht h2)

pressure in the left lamb above Y-Y = fix gx (shthi) + pa

Equating the pressures, we have $f_2 \times g \times (\Delta h + h_2) = P_1 \times 1 \times (\Delta h + h_1) + P_A$ $\Rightarrow P_A = P_2 g (\Delta h + h_2) - P_1 g (\Delta h + h_1)$ $\Rightarrow \Delta h (P_2 g - P_1 g) + h_2 P_2 g - h_1 P_1 g$

But from equation (i) , $\Delta h = \frac{a \times h_2}{A}$

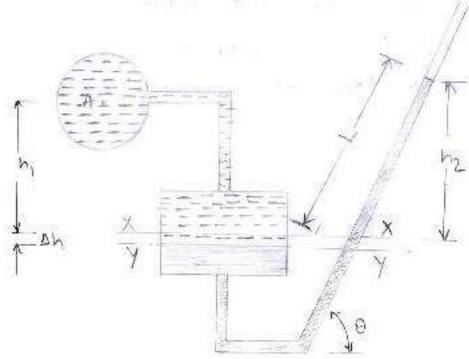
=> PA = axh2 [f2g-f19]+ hzf29- hif19 ----

As the area A is very large as compared to a hence traffor a becomes very small and can be neglected.

Then Pa = h2/29- h, fig :

from Loquetion not is clear that as he is known and hence by knowing he or raise of heavy liquid in the right limb, the pressure at A can be reglected Calculated.

[3] INCLINED SINGLE COLUMN MANDMETER >



The biguite shows the inclined single column manometer. This monometer is more sensitive. Due to inclination the distance moved by the heavy liquid in the reight limb will be more.

Let L = Length of heavy liquid moved in reight timb from X-X

0 = Inclination of reight limb with horizontal

hz= Ventical ruse of heavy loquid in reight limb from X-X = LX sing

From equation, the preciouse at A is

PA = h2f2g - h1f1g

Substituting the value of h2, we get
PA = Sin D x f2g - h1f1g

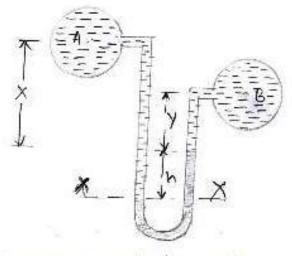
: DIFFERENTIAL MANDMETERS : -

Differential manometers are the devices used for measuring the chiffrenence of pressures between two points in a pipe on in two different pipes. A differential manometer consists of a U-tube, containing a heavy liquid, whose two ends are connected to the points, whose difference of pressure is to be measured. Most committy types of differential manometers are:

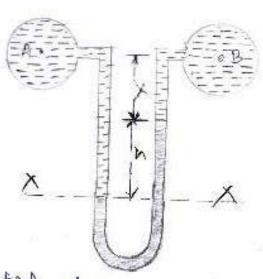
- (1) U-tube differential manometer and
- (3) Envented U-tube differential manometers.

(1) U-TUBE DIFFERENTIAL MANOMETER ?

The figures shows the differential manometers of U-tube type.



Coutwo pipes and distancent levels



(b) A and B are at same level

and also content logarids, of abbanent specific greavity. These points are connected to the U-tube differential manuscript. Let the pressure at A and B over Pa and Pa

Let he subsenence of meneury level in the U-tube,

y = Distance of the centre of Bitnom the more carry level in the night limb

X= Distance of the centre of A, brom the mercury level in the right limb

Pi = Density of liquid of A.

f2 = Density of liquid at B

fy = Density of heavy legald of mercany

Taking datum line of X-X.

Prossure above X-X in the left limb = f,g(h+x)+PA

where PA = Pressure at A.

Pressure above X-X in the right limb = fgxgxh+f2xgxy+pB where PB = pressure of B;

Equating the two pressure, we have

fig(htx)+PA = fgxgxh+f2gy+fB > PA-PB = fgxgxh*+f2gy-fig(h+x) = hxg(fg-fi)+f2gy-figx

Difference of pressure at A and B = hxg(fg-f1)+f294-f19x

Enfigure (b), the two points A and B are ed the same level and contains the Sume liquid of density for them

Pressure above X-X in right limb = fox g x h +fox g x x + po

Pressure above X-X in left limb = fox g x (h+x)+ Pa

Equating the two pressure

fg x g x h + P, gx + Ps = f, x g x h + x) + PA

=1PA - Ps = fg x g x h + f, g x - f, g (h + x)

= g x h (fg - f,)

[2] INVERTED U-TUBE DIFFERENTIAL MANOMETER-

It consists of an invended U-those containing a light liquid. The two ends of the two are connected to the points whose difference of pressure is to be measured. It is used for measuring difference of low pressures. The figure shows on invended U-tube differential managing Connected to the two, points A and B. 1801

Let the pressure at A is more than the pressure at B.

Lat hi= height of liquid milettimbs
below the doctor line X-X

hz=Height of liquid in relightlimb X h=Dibberrence of light liquid

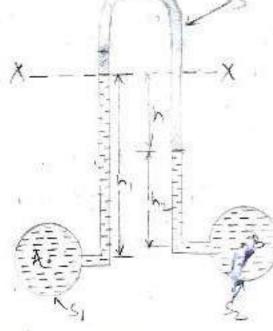
ti= Density of Deput of A

fz = Dansity ob liquid out B

Ps = Density of trapped light liquid

·PA = present at A

PB = Pressure out B



Taking X-X as datum line, then pressure in the left limb below X-X = PA-P, Xg Xh,

Presistance in the right limb below X-X
= RB- P2X 9 X h2- P5X 9 X h

Equating the two pressure,

PA-fixgxhi=Ps-tzxgxhz-tsxgxh

31B-PB=fixgxh1-f2xgxh2-f3xgxh

Questions?

(4) A simple V-tube monometers is used to measure the pressure of worders in a pipe line which is above the estimospheric of worders the wight timb obtain monometers contains moneung it is upon to the older pressure A the contact between u the big determine the pressure of moneung seconds is to the less that we share in the two of the old the determine the less of the the the less of the

tig is not the same level on the center of the pipe? Ons) PATPI 9hi = Paghe

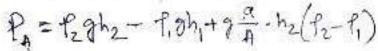
=>PA + (1000 × 9.81 × 10 × 10-2) = (13.6 × 1000 × 9.81 × 100 × 10.2) =>PA = (1000 × 9.81 × 1000 × 9.81 × 1000 × 9.81 × 1000 × 9.81 × 10 × 10-3)

7 PA = 133416- 981 = 12360.6 N/m² (Ans)

(3) A single column monometer is connected to a pape containing a liquid of specific flavity or as shown in biguing. find the pressure on the pape it the area of the mercentain is looking the area of the mercentain is looking the area of the fire area of the fire area of the fire area of the mercentain is looking the area of the area of the fire area of the containing the area of the area of the fire area of the fire area of the area

20

(Ans) $h_1 = 20 \, \text{cm} = 0.20 \, \text{m}$ $h_2 = 40 \, \text{cm} = 0.4 \, \text{m}$ $f_1 = 0.9 \, \text{x} \, 1000 = 900 \cdot$ $f_2 = 13.6 \, \text{x} \, 1000 = 13600$ $f_2 = 9.81$





A=lova

=100

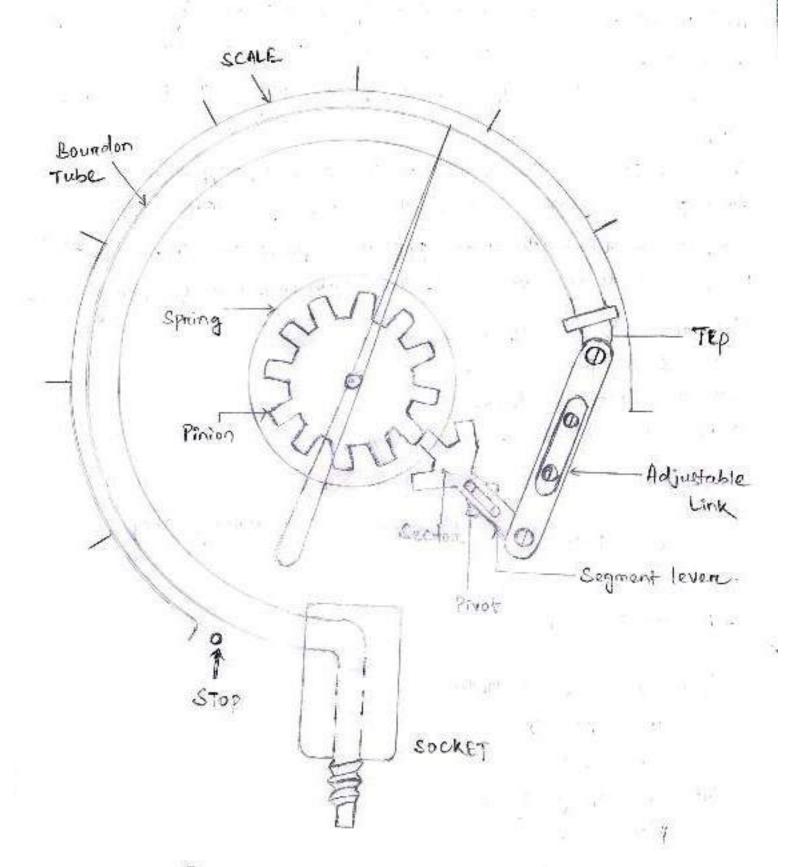
= 13600x9,81 x0.4-900x9.81 x0.21+ 9.81 x 100 x0.4(13600-900) = 53366.4-17658+0.03924 x 12700

= 35.708.4 4498.348

= 36206-748 N/m2 (Ans)

BOURDON TUBE PRESSURE GAUGE

- Theoreton tube pressure gauges are classified as mechanical pressure measuring instrument, and thus operate without any electrical power. This type of pressure gauges were first developed by E. Bourdon in 1849.
- 7 Bounday tubes one madially formed tubes with an oval
- Thousand tube pressure gargages can be used to measure over a wide mange of pressure form various to pressure as high as few thousand psi.
- 7 It is basically consisted of a C-shaped hollow tube, whose one end is fixed and connected to the pressure tapping, the other end tree.
- -7-The Cross Section of the two is elliptical. When pressure is applied, the elliptical tabe (Bounder tube) tries to acquire a cincular Cross-Section, as a result, Stress is developed and the two tries to Stresgitten up.
- magnitude of pressure.
- This motion is the measure of the pressure and is indicated via the movement of a deflecting and indicating mechanism is attached to the bree end that retates the pointer and indicates the pressure reading.
- orthe materials used are commonly phosphore Bronze, Breaks and Berrylloum, Copper.
- tubes, such as helocal, twisted on spiral tubes are also in use.



[BOURDON TUBE PRESSURE GAUGE]

CHAPTER - 03 TOTAL PRESSURE AND CENTRE OF PRESSURE =

or Total pressure is defined as the funce exercted by a staticity on a sunface esther plane on Curved when the blued in contact with the sunfaces. This force always acts normal to the Surface "

-7 Centre of pressure is defined as the point of application of the total pressure on the sunface. There are four cases of submerg Sunfaces on which the total pressure force and centre of pressure is to be determined. The Submerged sunfaces may be ;

(1) Vertical plane Surface

- (2) Horizontal plane surface
- (3) Inclined plane surface
- (4) Curved surface

(1) Ventical plane sunface submerged in Liquid of

Consider a plane Ventical sunface of consisterary shape immercial in a liquid as shown in biguire.

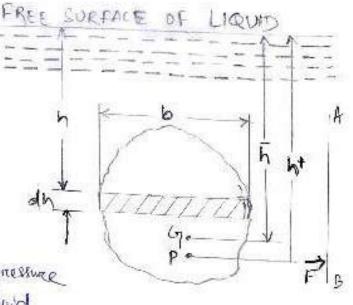
Let A = Total area of the Surface_

> h 7 Distance of C.G. of the anea brown breez surface of lequid

G = central of growity of plane Surface.

P = centre of pressure

W = Distance of Centre of pressure prom pres rankants of redució



(a) TOTAL PRESSURE (F) :-

The total pressure on the surface may be bletermined by abstracting the entire surface into a number of small parallel strips. The force on Small strip is then calculated and the total pressure bonce on the whole area is calculated by integrating the force on Small strip;

Consider a strip of thickness with and width to at the depth of h brom bree surface of liquid as shown in bigure.

pressure intensity on the strop, p=figh Area of the Strop, dA = bxdh

Total pressure bonce on strip, df = px Area = fghxbxdh

. Total pressure borre on the whole surface,

F= fdF=ffghxbxdh=fgsbxhxdh

But Soxhxdh = ShxdA

= moment of surface cinea about the bree Surface of logical

- Area of surface × Distance of e.g. 5mm the brice surface

= AX h

+ F= Pg AT

I force would be in Newton.

(b) Centre of Pressure (h') :-

Centre of pressure is calculated by using the principle of money, which states that the moment of the resultant bonce about an axas is equal to the sum of moments of the components about the same axis.

The resultant force F is acting at p, at a distance hi brombree surface of the legal as shown in figure. Hence moment of the borce F about three surface of the liquid = F x h' — (1)

Moment of force of, acting on a strip about bree surface of legal = df x h

[: df = pqh x b x dh]

= fqh x b x dh x h

Sum of moments of all such borces about free Surface of liquid

= offices (fghxbxdhxh

= fg (bxahxholh

+ Pa (usu)

= 9 Statedh = 9 sh2dA (": bdh=dA)

But ShadA = Sbhadh

= moment of Ineration of the surface about the free surface of legal = Io

: Sum of moments about bree surface = fg10 - (2)

Equating (1) and (2), we get

FX h' = fg 20 But = F = fg A h

:. fgmx h = fg10

 $\Rightarrow h' = \frac{fg\tau_0}{fgAh} = \frac{\tau_0}{Ah} \qquad (3)$

By the theorem of parallel axis, we have Io = Tythax h2

where In moment of Inentice of the about an axe passing through the city of the anen and parallel to the free surface of legald.

Substituting To in equation (3), we get $h' = \frac{I_0 + Ah^2}{Ah} = \frac{I_0}{Ah} + h \qquad (4)$

In egn 14), it is the destance of cigob the area of the ventical surface from the surface of the liquid. Hence from equation (4), it is clear that

(1) Certae of passione (i.e. h!) has bottom the certae of gravity of the vertical surface.

(ii) The distance of centre of pressure been three surface of liquid is independent of the density of the liquid.

The Moments of Inertia and other geometric properties of Some Important Plane Surfaces:

Plane Surface	C.G. brom	Arren	Moment of Inerctic about an axis passing through E by, and I parallel to bate (Iby)	thoment of inerotic about base (ID)
1. Rectangle	n = d	Ьď	bd3	<u>543</u>
7. Traingle	x= 1/3	<u>bh</u> 2	<u>bh³</u> 36	443 12

Plane Sunface	C-Gy. brom the Base	Ane a	stonent of mentice about an axis passing through C.G. and parallel to base (Ig)	Laco for
83. Cincle	2=d	742 4	TING TO	
4. Trapezium	2a+b)h	(a+b); h	(a2+4ab+b2)xh3 3b(a+b)	

ARCHIMEDES' PRINCIPLE

- of When an object is completely on particulty immensed in a bluid, the bluid exents an appeared borce on the object equal to the weight of the bluid displaced by the object.
- of when a solid object is wholly on printly immersed in a blood, the bluid molecules are continually striking the Submerged Surface of the object. The force due to these impacts can be combined into a single borce the buoyant force. The immersed object will be lighter to the buoyant of buoyand up by an amount equal to the weight of the build it displaces.

BUOYANCY >

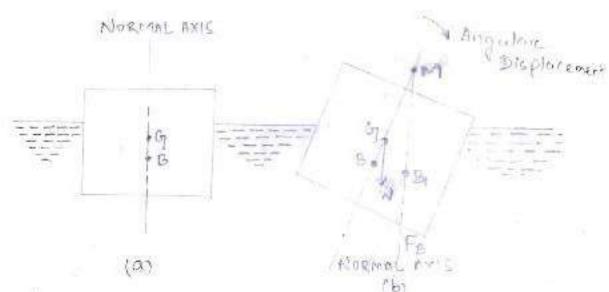
When a body is immensed in a bluid, an upround bornce is exented by the bluid on the body. This upward bornce is equal to the weight of the bluid displaced by the body and is called the bornce of belogancy on Simply buoyancy.

CENTRE OF BUDYANCY :-

It is defined as the point, through which the force of buoyancy is supposed to act. As the force of buoyancy is a vertical force and is equal to the weight of the fluid displaced by the body, the Centre of buoyancy will be the centre of gravity of the fluid displaced.

oscillating when the body is tilted by a small angle. The meta-current may also be defined on the point at which the line of action of the force of bouryancy will meet the nound axis of the body when the body is given a small angular olisplacement.

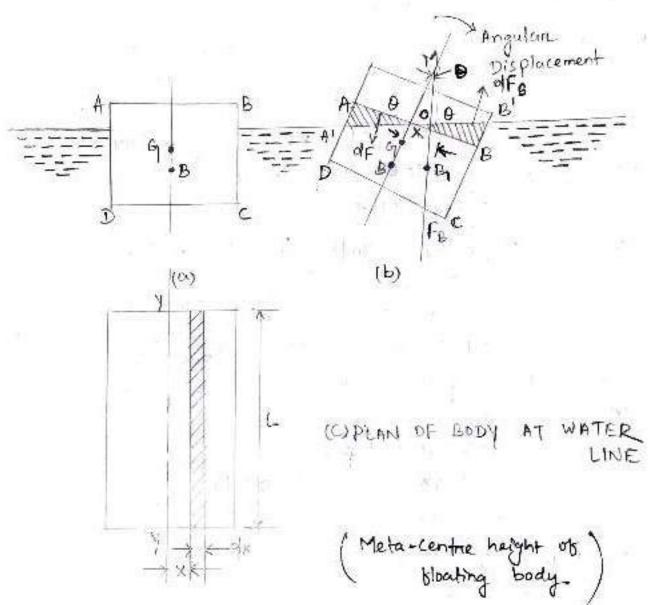
The Considere or body bloating in a liquid as shown in figure. Let the body is in equilibrium and by is the centre of greavity and bithe Centre of buoyancy. For equilibrium, both the points lie on the normal axis, which is Nentical.



Let the bedy is given a small angular displacement in the clockwise direction as shown in bigure (a). The Centre of buoyancy, which is the centre of gravity of the displaced liquid on Centre of gravity of the poster of the body sub-merged in liquid wall now be shifted towards right from the normal axis, Let it at a as shown in bigure (b). The line of action of the force of buoyancy in this new position, will intensect the normal axis of the body out some point say M. This point M is called Meta-Centre.

META-CENTRIC HEIGHT &

The distance Mg, i.e. the distance between the meta-centre of a bloating body and the centre of gravity of the body is called meta-centric height.



Comple Due to Wedges :-

Consider towards the right of the axis a small strop of thickness also at a distance of a from D as shown in bigkb.

The height of strop ** X LBOB! = X X O (:: LBOB! = LAOA! = BMB! = 10)

2. Arrea of strap = Height X Thickness = XXBXdX

96 L is the length of the bloating body other

Volume of strap = Arrea X L

= XXBXLXda

*. Weight of strop = if g x volume = for oldar

Simplantly, it a small strip of thickness du at a distance or from O to wands the left of the axis is considered, the weight of strip up be flynould a. The two weights one outling in the apposite direction and hence constitute a couple.

Moment of this emple = Weight of each strop x Distance between these two weights

= four Lan x 2n = 2 fgn2 ol da

:. Moment of the couple for the whole wedge = \$2590x2 a Late -(1)

Moment of couple due to shifting of Centre of buoyancy trum

B to B | = FB x BB |

= FB x BM x 0 (-1 BB = IBM x 0 if 0 is very

= W x BM x 0 —(2) (FB = W)

But these two couples care the same thence equating equations

WXBMXB = Separzolda NXBMXB = 12fgo Sarabalda NXBM = 2fg Sarlda

Now Lange Elemental arrest on the water fine shown in figure (c) and = all

is MX BW = 368 las oft

But from figure (c). it is clear that 2 (n2 old is the second moment of area of the plan of the body out whater surface cubout the axis y-y. Therefore

WXBM=fgE => BM= fgI W (where L = 2 for 2014)

But 'W = weight of the body

= weight of the bland dispinced by the body

= 49 x Volume of the bland displaced by the body

= fg x Volume of the body Sub-merged in water

= fg x V

: BM = \frac{4}{7}xI = \frac{1}{4} - (3)

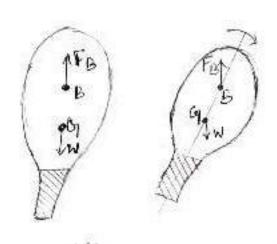
GM = BM - BG = \frac{1}{4} - BG = \frac{1}{4} - BG = (4)

: Metal Central height = GM = \frac{1}{4} - BG = (4)

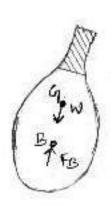
CONDITIONS OF EQUILIBRIUM OF A FLOATING AND
SUB-MERGED BODIES

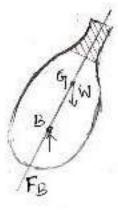
A sub-merged on a floating body is said to be struble it it comes back to its original position after a slight disturbance. The relative position of the centre of gravity (6) and centre of buoyancy (8) of a body determines the Stability of a sub-merced body.

The position of Centre of gravity and centre of buoyancy in case of a Completely submerged body are fixed. Consider a balloon, which is completely submerged in air. Let the lower portion of the bearganty balloon centains heavier material. So that its Centre of gravity is lower than its centre of buoyancy as shown in figure (a). Let the weight of the balloon is W. The weight Wis acting through by verifically in the douonicand direction, while the bruoyant force Fo is acting verdically up, through B. For the equilibrium of the balloon w= Fo. If the balloon is given an angular displacement in the Clockwise alirection as shown in bigure (a), then w and Fo konstitute a couple acting in the anti-clockwise alirection and brings the balloon in the original position. Thus the balloon in the position, shown by bigure (cy is in Stable equilibrium.

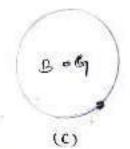


(4) STABLE EQUILIBRIUM





(b) EQUILIBRIUM UNSTABLE



NEUTRAL EQUILIBRIUM

(Stabilities of Jub-marged bodies)

(a) Stuble Equilibrium -

When W= Fg and point is is above by, the body De said to be in stable equalibrium.

(b) Unstable Equilibration 1—

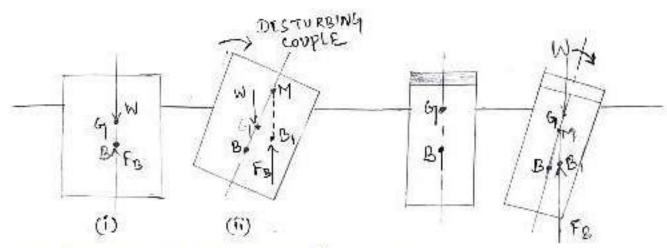
If W= Fg. but the centre of buoyancy (B) is below tentre of gravity (h), the body is in unstable equilibration as shown in fig(b). A slight displacement to the body in the clockwise disceedion to the body. In the clockwise direction, gives the couple due to Way Fig also in the clockwise direction. This the body does not refun to its original position and too hence the body is in unstable equillobrium.

(c) Neutral equilibratum 9—

It FB = W and B and by one at the same point, as shown in big takes, the body is said to be in neutral equilibration.

* Stability of Floating Body =>

The stubility of a bloating body is determined from the position of Meta-centre (M). In case of bloating body, the weight of loguid displaced.



(a) Stable equilibration M is above by

(b) Unistable equilibration of

(Stability of Housing bodies)

(a) Stable Equilibrium:

If the point M is above M is above by, the blooking body will be in stable equilibrium as shown in by (a). It a slight angular displacement is given to the blooking body is the clockwise direction, the Centre of buoyancy shifts from B to B, such that the vertical line through By eats at the then the blooking in the arti-clockwise elinection and thus bringing the blooking in the arti-clockwise elinection and thus bringing the blooking the blooking body in the original position.

(b) Unstable Equilibrium 2

The the point m is below G, the bloating body will be in unstable equilibrium as shown in (b). The disturbing couple is acting in the alcoholise direction. The comple due to buoyant bonce F3 and w is also acting in the clockwise alerection and thus overcturning the bloating body.

is Newtral Equilibrium:

The the point my is out the centre of greavity of the body, the bloating body will be in neutral equilibrium.



TYPES OF FLUID FLOW: -

The bluid flow is classified as a

- (i) Steady and unsteady blows
- (ii) Uniform and non-uniform Hows
- (iii) Laminar and turbulent blows
- (in compressible and incompressible flows
- (N) Rotational and irrectational blows and
- (Ni) One, two or three domensional blows

(1) Steady and Unsteady blows >

Therapy blow is defined as that type of blow in which the blowd Characteristics like volocity, pressure, density etc. at a point do not change with time the bore steady blow, mathematically, we have

whome (xo, yo, zo) is a boxed point in blund bield

The density a respect to time, Thus modhernatically, for unsteady fier

(1) Uniform and Non-Uniform Flows of

Velocity of any given time does not change with respect to space the Congth of direction of the blow). Mosther modically, bore uniform the

where ov = change ob velocity

Bs = Length of blow in the direction s

of Non-Uniterior Blow is that type of blow in which the velocity of ciny given time Changes with respect to space. Thus, mathematically, box non-uniform blow

(Ss) t= constant # D

(iii) Laminan and Turbulent Flow >

- Pareticles move along well-defined paths on steam line and all the steam lines and parallel. Thus the pareticles move in laminas on layers gliding smoothly over the adjacent layer. This type of blow is also called steam-line blow or viseous blow.
- Turbulent blow is that type of blow in which the bluid pandicles move in a zig-zag way. Due to the movement of bluid pandicles on a zig-zag way, the eddies formation tokes place which are responsible for high energy loss. For a pope blow, the type of blow is determined by a non-dimensional number. Called the Reynold number.

where D = Documeter of pipe

N= mean velocity of blow on pipe

V = Kinematic Viscocity of Bluid

laminant. It the Reyland number is more than 4000, then it is called turbulent blow. It the Reyland number is more than 4000, then it is called turbulent blow. It the Reynold number lies between 2000 and 4000, the flow may be laminant on turbulent.

(IV) Compressible and Pricompressible Flows of

"T Compressible blow is that type of blow in which the dentity of the bluid changes brown point to point on in other words the dentity of the bluid. Thus, madhematically, fore (P) is not constant from the bluid. Thus, madhematically, fore (P) is not constant from the bluid. Thus, madhematically, fore (P) is not constant from the bluid.

of & constant

-1) Incompressible blow is thed type of blow in which the density is constant bouthe Bluid blow. Liquids age generally incompressible cohile gases are compressible. Mathematically, box a incompressible blow:

F = constant

(V) Rotational and Pretrotational Flows >

Rotentional blow is that type of blow in which the bluid particles while blowing along steam times, also restates about their can axis. And, it the bluid particles while blowing along steam lines, do not restate about their own axis then that type of blow is earlied innestational blows

Vi) One-, Two-, and Three-Dimensional Flows :-

The dimonstronal blow is that type of blow in which the blow parameter such as velocity is a function of time and one space ephordinate only say at for a steady one, dimensional blow, the velocity is a bunchion of one space. Co-credinate only. The vertication of velocities in other two mutually perpendicular abaction is outstuned negligible. Hence, mathematically, for one-dimensional blow,

u= 5(a), v=0 and w=0

when u, v. and we are velocity components in a, y and z directions mespectively,

Two-observational blow is that type of blow in which the velocity is a faceth bunction of time and two rectangular space co-ordinates or constant say or and y. For a steady two-dimensional blow the velocity is a function of two-space co-ordinate only. The velocity of velocity in the third dimensional blow, negligible. Thus mathematically for two-dimensional blow, it is negligible. Thus mathematically for two-dimensional blow,

-1 Three-dimensional blow is that type of blow in which the velocity is a bunction of time and three mutually perpendicular directions. But bor a steady three-dimensional blow the bluid parameters are bunctions of three space co-ordinates (14, y and 2) only. Thus, mathematically, bor three-dimensional blow, we blow, we be bounded to be blowday.

RATE OF FLOW OR DISCHARGE (Q)

It is defined as the quantity of a fluid blowing per second through a section of a pape on a channel. For an incompressible blood (on location) the node of klow on dischange is expressed as the volume of blood blowing excross the section per second. For compressible bloods of the nate of blow is usually expressed as the weight of blood blowing extrass the section. Thus (i) for loquids the Units of Q are m3/s or latres/s

(ii) for gases the units of Q is kg f /s on Newton/s

Consider a loqued blowing through a pape in which

A = Causs-Sectional area of Pipe

A = Cours - sectional

V= Average velocity of bluid econoss the section

Then Discharge Q = AXV.

CONTINUITY EQUATION ?

The equation based on the principle of Conservation of maks is called Confinulty Equation. That for a blaid blowing through the pipe of all the cross-section, the quantity of blud per second is constant. Consider two enver-sections of a pape as shown in bigues; Let V, = Average velocity at Cross-Section 1-1 -P1 = Density out section 1-1 A = Area of Pipe at Section 1-1

and V21 f21 Az are cornesponding value at section 2.

Then note of blow ed section 1-1= P. A.V.

Right of Stow out Section \$2-2 = P2 Az V2 of Flow According to law of Conservation of TOOSH.

Rede of blow at section 1-1

Fluid blowing through

= Rate of blow out section 2-2

19,A14 = P2 A2V2

The above equation is supplicable to the compressible as well as incompressible bluds and is called Continuity Equation. If the blud monoto is incompressable,

then of = f2 and continuity equation revoluces to

A, V1 = A2 V2

EQUATIONS OF MOTION ?

According to Newton's Second low of motion, the net fonce Fix acting on a bluid element in the direction of it is equal to make in of the Bluid element multiplied by the acceleration.

Axin the x-direction,

Thus mathematically; Fx = m-an

In the fluid blow, the following brances are present,

(i) Fg, gravity borce

(ii) fp, the pressure borce

(10) Fr, bonce due to Viscosity.

(i) For borne due to tumbulence

(4) Fc, bonce due to compressibility

Thus in equation, the net boace

Fx = (Fg) n + (Fp) n + (Fv) on + (Fe) at (Fc) x

(i) It the bonce due to compressibility, fe is negligible, the nesulting net boace

Fx = (Fg) nx + (Fp) nx + (Fv) nx + (Fd) n

and equation of motions are called Reynold's equations of motion.

- (ii) For blow, where (F4) is negligible, the mequed equation resulting equations of motion are known as Navier-Stokes Equation.
- (ii) It the blow is assumed to be ideal, this cous borce (Fv) is zero and equation of motions are known as Euler's equation of mation.

EULER'S EQUATION OF MOTION ?

This is equation of motion in which the borce flue to gravity and pressure are taken into consideration. This is dereaved by considering the motion of a bluid element along a stream-line as "

consider a stream-line in which blow is taking place in a discretion as shown in biguine. Consider a Cylindrical element of Cross-section as shown in biguine. Consider a Cylindrical element or character acting on the Cylindrical element are

1. pressure bonce pdf in the director of 5000

2. Pressure force (p+ &p ds) dA opposte to the direction of blow, a weight of element padAds.

Let 0 is the angle between the ofinection of blow and the line of action of the weight of element.

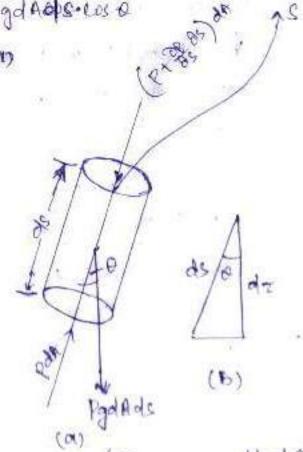
The resultant borcce on the bluid element in the direction of os must be equal to the mass of bluid element X acceleration in the direction s.

= fdAds xas - (1)

on the direction of s.

Now, $a_s = \frac{dv}{dt}$, where v is a bundom of s and t.

It the flow is steady,



Substituting the value of Cis in agri (1) and simplifying the equation, we get

- OP alsola - Py dads cost - poladsx of

Dividing by PoledA, -- ap -g cos a = vdv

on de + g cos 0 + V dy =0

But from tig(tb), we have cos o = ots

Equation (2) To known as Eulen's equation of motion.

BERNOULLI'S EQUATION FROM EULER'S EQUATION >

Bennoulliss equation is obtained by integrating the Euler's equation of motion as

of blow is incompressible, fire constant and

$$\frac{P}{P} + gz + \frac{v^2}{z} = constant$$

= Pg + Z + \frac{\sqrt{2}}{29} = lon stant

$$\Rightarrow \frac{p}{fg} + \frac{v^2}{2\eta} + Z = constant \qquad (9)$$

Equation (3) is a Bernoulli's equation in which,

Pg = pressure energy per unit weight of third on pressure head

V2/2g = kinetic energy per unit weight on lanetic head Z = potential energy per unit weight on potential head

ASSUMPTIONS :-

The following one the assumptions made in the devilvation of Berenoulli's equation:

(i) The bluid is ridealine. Viscosity is Zeno.

(6) The How is Steady.

(iii) The Blow is in compressible.

(14) The blow is Ircrotational.

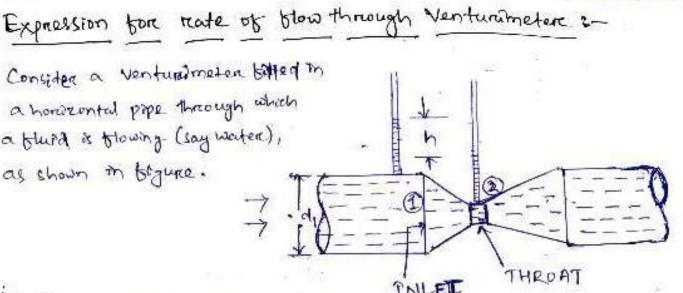
PRACTICAL APPLICATIONS OF BERNOULLI'S EQUATION:

Bernoullis equation is applied in all problems of incompressible blud blow where energy considerations are involved. But we shall consider its application to the bollowing measuring devices:

- 1. Venturimeter
- 2. Orabbice meters
- 3. Pitot tube

(1) Venturimeter =>

- of a bluid blowing through a pipe. It consists of three parts in
 - (1) A short converging point,
 - (1) Throat and (iii) Diverging parit.
- 7 94 his based on the principle of Bernowliss equation.



Let P1 = pressure out section (1)

d1 = eliameter out inlet on out

contion (1).

[VENTURIM ETER]

VI = velocity of bluid on section (1), a = Area at section (1) = 1 4,2

and d2, P2, V2, a2 are courses ponding values at section (2).

Applying Beaumoullist equation at section (1) and (2), we get

As pope is horazontal, hence = Z= Zz

:.
$$\frac{P_1}{P_9} + \frac{V_1^2}{2g} = \frac{P_2}{P_9} + \frac{V_2^2}{2g}$$
 or $\frac{P_1 - P_2}{P_9} = \frac{V_2^2}{2g} - \frac{V_1^2}{2g}$

But PI-Pz is the dibterence of pressure heads at soctions found 2 and it is equal to hore PI-Pz = h

Substituting this value of PIP2 in the above equation, we get

$$h = \frac{V_1^2}{2g} - \frac{V_1^2}{2g}$$
 - (5)

Now applying continuity equation at section 182 a, v = a2 v2 on v, = a2 v2

$$h = \frac{v_2^2}{2g} = \frac{\left(\frac{a_2 v_2}{\alpha_1}\right)^2}{\frac{2g}{2g}}$$

$$= \frac{v_2^2}{2g} = \frac{\left(1 - \frac{\alpha_2^2}{\alpha_1^2}\right)^2}{\frac{2g}{2g}} = \frac{v_2^2}{\frac{2g}{2g}} \left(\frac{\alpha_1^2 - \alpha_2^2}{\alpha_1^2}\right)$$

$$\Rightarrow v_2^2 = \frac{2gh}{\alpha_1^2 - \alpha_2^2} = \frac{\alpha_1}{\alpha_1^2 - \alpha_2^2}$$

$$\Rightarrow v_2 = \sqrt{2gh} = \frac{\alpha_1^2}{\alpha_1^2 - \alpha_2^2} = \frac{\alpha_1}{\alpha_1^2 - \alpha_2^2} = \sqrt{2gh}$$

. Discharge, Q = a2 V2

$$= \frac{a_2}{A_1^2 - a_2^2} \times \sqrt{2gh}$$
=7 $Q = \frac{a_1}{\sqrt{a_1^2 - a_2^2}} \times \sqrt{2gh} - -(6)$

Equation(6) gives the discharge under rideal conditions and is called theoretical discharge. Actual discharge will be less than theoretical discharge.

where ey= co. efficient of Venturismeter and its value is less .

than 1. (co-efficient of discharge)

Value of the givenby different to tube manometers >-

Case-1: Let the distremential monometers contains a liquid which is heavier than the liquid blowing through the pipe.

Let Sh = Specifix growthy of the heavier liquid

So = specific growthy of the liquid flowing through pipe

N = Specific growthy of the heavier liquid column in U-tube

Case-11: 25 the differential manameters tentains a layured which is lighters. Than the liquid blowing through the pipe, the value of his given by,

h = x [1- se]

Se = specific greatity of bojoinlighter liquid in U-tube

So = specific greatity of blund blowing through Pipe

R = Difference of the lighter liquid columns in U-tube.

Decestions The diameter of pipe at section 1 & 2 and to cm & 15 cm nespectively. Find the directions through the pipe, it the velocity of worker flowing through the pipe of section 1 is 5 m/s. Also determine the velocity at section 2.

Answer: - $d_1 = 10 \text{ cm}, d_2 = 15 \text{ cm} = 3.15 \text{ m}$ $V_1 = 5 \text{ m/s}$ $V_2 = 23$ $Q_1 = 77$

 $\begin{cases}
Q_1 = A_1 \times V_1 \\
= \frac{\pi}{4} d_1^2 \times V_1 \\
= \frac{\pi}{4} (b_1)^2 \times 5 = \frac{\pi}{4} \times b_2^{\frac{10}{10}} \times 5 = 3.141 \times 125 \\
= \frac{\pi}{4} \times (b_1)^2 \times 5 = \frac{\pi}{4} \times b_2^{\frac{10}{10}} \times 5 = 3.141 \times 125$

 $Q_{1} = \frac{11}{4} \times 10.001 \times 5$ $= \frac{11}{4} \times 0.0001 \times 5$ $= \frac{3.141}{4} \times 0.0001 \times 5$ $= 0.0342 \text{ m}^{3}/5$

Then, A, VI = A2V2 0.03.92 0.03.92 0.0392 0.0392 0.0392 0.0392 0.0392 0.0175

The Go cm. diameter pipe in which water is blowing branche, into two pipes of diameter 20 cm. and 15 cm respectively.

Of the average velocity in the 30 cm. diameter pipe is 25 m/s, findout the discharge in the pipe? Also determine 25 m/s, bindout the discharge in the pipe? Also determine the velocity in 15 cm. pipe if the average velocity in 20 cm. the velocity in 15 cm. pipe if the average velocity in 20 cm. diameter pipe is 2 m/s?

Any Given, $d_1 = 80 \text{ cm} = 0.30 \text{ m}$ $d_2 = 20 \text{ cm} = 0.20 \text{ m}$ $d_3 = 15 \text{ cm} = 0.15 \text{ m}$ $V_1 = 2.5 \text{ m/s}$ $V_2 = 2 \text{ m/s}$ $V_3 = 2?$

 $V_2 = 2\pi I_5$ $V_3 = 2?$ $Q_1 = A_1 \times V_1$ $= \frac{\pi}{4} A_1^2 \times V_1$ $= \frac{\pi}{4} \times (0.30)^2 \times 245$ $= \frac{\pi}{4} \times 0.09 \times 2.5 = \frac{3141}{4} \times 0.09 \times 2.5$ $= 0.76 \times 0.09 \times 2.5$

= 0.176 m3/s

In tigune, Q1=Q2+Q3 >> A1V1 = A2V2+A3V3

70-176 = #xd2xv2 + # Txd3 xv3

= \$x 6.20) 2x 2 + \$x (0.15 } x'V3

= 0.78 x 0.04 x 2 x + \$0.78 x 0.0225 x V3

=>0.176 =0.0624 + 0.0175 xv3

70-196-10.0624 = 0.0175 XV3

1 7 0.1136 =0.0175 XN3

$$V_{3} = \frac{0.1186}{0.0175}$$

$$\Rightarrow V_{3} = 6.4 \text{ m/s} \quad (Ans)$$

$$OR, \quad Q_{1} = Q_{2} + Q_{2}$$

$$\Rightarrow A_{1}V_{1} = A_{2}V_{2} + A_{3}V_{3}$$

$$\Rightarrow A_{1}V_{1} = A_{1}V_{2} + A_{2}V_{3} + A_{2}V_{3} + A_{3}V_{3}$$

$$\Rightarrow A_{1}V_{1} = A_{1}V_{2} + A_{2}V_{3} + A_{2}V_{3} + A_{3}V_{3}$$

$$\Rightarrow A_{1}V_{1} = A_{1}V_{2} + A_{2}V_{3}$$

$$\Rightarrow A_{1}V_{1} = A_{2}V_{2} + A_{2}V_{3}$$

$$\Rightarrow A_{1}V_{1} = A_{2}V_{1} + A_{2}V_{2}$$

$$\Rightarrow A_{1}V_{1} = A$$

$$V_{AB} = 3m/s$$
 $Q_{AB} = ?$
 $Q_{AB} = ?$
 $Q_{CE} = ?$
 $Q_{CD} = \frac{1}{2}Q_{AB}$
 $Q_{CE} = \frac{1}{3}Q_{AB}$
 $Q_{CE} = \frac{1}{3}Q_{AB}$

Rate of discharge at AB,

$$Q_{AB} = A_{AB} \times V_{AB}$$

$$= \frac{\pi}{4} (d_{AB})^2 \times V_{AB}$$

$$= \frac{\pi}{4} (1.2)^2 \times 3 = \frac{\pi}{4} \times 1.44 \times 3 = 0.76 \times 3 \times 1.44$$

$$= \frac{\pi}{4} (1.2)^2 \times 3 = \frac{\pi}{4} \times 1.44 \times 3 = 0.76 \times 3 \times 1.44$$

$$= \frac{\pi}{4} (1.2)^2 \times 3 = \frac{\pi}{4} \times 1.44 \times 3 = 0.76 \times 3 \times 1.44$$

From bigune, and and QAB = QBC

THANK VAB = ABC X VBC

THOMAN X VAB = TX (CBC) 2 X VBC

TY (CHAB) X X 3 = TX (CBC) 2 X VBC

TY (CHAB) X X 3 = TX X (CBC) 2 X VBC

=> 3.39 = 1.76 × VBE => VBC = 3.39 = 1.92 m/s 1.76 = 1.76 = 1.92 m/s 1. Velocity in BC is 1-92 m/s Then, Qep = 3 Rm = 3 × 3.39 = 1.131 m3/s

 $Q_{CE} = Q_{AB} - Q_{CD} = 3.39 - 1.131 = 2.262 m^3/5$ OR $Q_{CE} = \frac{2}{3}Q_{AB} = \frac{1}{3} \times 3.39 = 2.262 m^3/5$

Velocity for CD ...

$$V_{CD} = \frac{Q_{CD}}{A_{CD}}$$
 $V_{CD} = \frac{Q_{CD}}{A_{CD}}$
 $V_{CD} = \frac{Q_{CD}}{A_{CD}}$

7 Nep = 2-25 m/s 1. Nelocity in CD is 2.25 m/s

diameter of CE can get from this expression,

we know, Discharge out CE,

QUE = ACEX VCE

7 Que = Tx(die)2 x VCE

> 2.262 = = = x (dec) x 2.5

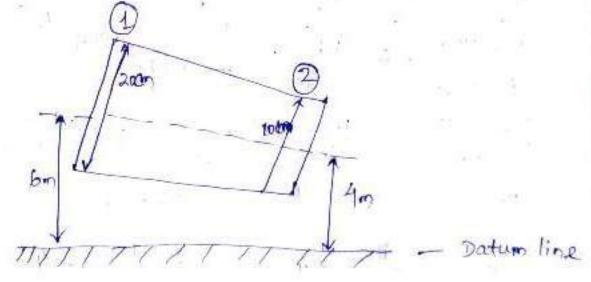
>> 2.262 = (dcs)2 x 1.963

7 (des) = 2.262

= 1-073 m.

: diameter of CE is 1-073 m.

1 Water is blowing through a pipe having diameter 20 cm. & 10 cm at section 122 nespectively. The nate of blow through page is 35 litrefsel. The section 1 is 6 m, above the datum and section 2 is 4 mr above the datum. If the pressure at cross section 1 is 39.24 Alone other bind out the fundencity of pressure out section 2.



Given, d= 20 cm, = 0,20 m Z, = 6m. 0/2= 10 cm, =0,10m = 72=4m. Q= 3545 . . 9 = 9-81 7 Q = 35×10-3 m3/5 f= 1000 kg/m2 P1=39.24 N/cm2 = 39.24 × 104 N/m2. According to Bernoul's equations. +71+ V12 - P2 + Z2+ 129 - 199 + Z2+ 129 Q=Q= Q = 35 e/s Q = A, V, 735×10-3= 7×607×4 = Tx(0.20) x Y =0.78 XD.01 XV2 735 X 10 3 = 0.78 KO.04 XV 9 35x 103 = 0.0312 XV 7 0.035 = 0.0312XV Then according to Bernowts equation, >> 2929× 107 + 6 + 1.21 = P2 + 4+ 19.36 9810 + 4+ 19.62 $970+6+0.061 = P_2 + 1+0.986$ $970+6+0.061 = 9810 + 4.986 <math>9 P_2 = 41.075$

$$= 102945.75 \times 9810$$

= 402945.75 N/m²
= 40.29 N/cm² (And)

(B) An oil of specific greavity 0-8 is blowing through a .

Venturimeter having in let cliameter 20 cm. and throught

Venturimeter having in let cliameter 20 cm. and throught

diameter 10 cm. The oil francury differential manameters

diameter 10 cm. The oil francury differential manameters

shows a reading of 25 cm. Calculate the discharge of

shows a reading of 25 cm. Calculate taking Cd = 0-98?

(my) Given, of = 20 cm = 0.20 m

$$d_2 = 10 \text{ cm} = 0.10 \text{ m}$$

$$S_{12} = \text{specific growity of oil} = 0.8$$

$$S_{13} = \text{specific growity of mencury} = 13.6$$

$$S_{14} = \text{specific growity of mencury} = 13.6$$

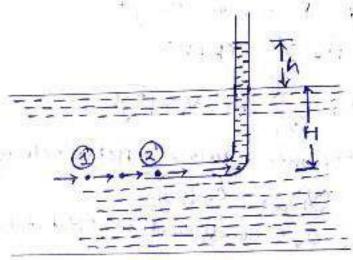
$$S_{15} = \text{specific growity} = 25 \text{ cm} = 0.25 \text{ m}$$

$$S_{15} = \text{specific growity} = 25 \text{ cm} = 0.25 \text{ m}$$

According to case - I,

$$h = \pi \left[\frac{sh}{sn} - 1 \right]$$
= 0.25 x \left(\frac{13.6}{0.8} - 1 \right) = 0.25 x (17-1) = 0.25 x 16
= 40 cm

It is a device used for measuring the velocity of blow at any point in a pipe or a channel . It is based on the principle point in a pipe or a channel . It is based on the principle that it the velocity of blow at a point becomes zero, that it the velocity of blow at a point becomes zero, that it the pressure there is increased due to the conversion of the kinetic energy into pressure energy. In its simplest form, the pitot-tube consists of a glass tube, bent at rught angles as shown in biguire.



Pitot-tube

The lower and, which is bent through 90° is directed in the up steam direction as shown in figure. The liquid rises up in the tube due to the conversion of kinetic energy into pressure energy. The velocity is determined by measuring the rise of liquid in the tube.

Consider two points (1) and (2) at the same level in such a way that point (2) is just as the inlet of the pitot-tube and point (1) is bak away from the tube.

Let P1 = intensity of processure cut point (1)

M = velocity of flow at (1)

P2: processure at point (2)

V2 = velocity out point (2), which is Zero

H = elepth of tube in the liquid

h = rise of liquid in the tube cubove the free surface.

Applying Bernouti's equation at points (1) and (2), we get

$$\frac{P_1}{P_0} + \frac{\sqrt{2}}{29} + Z_1 = \frac{P_2}{P_0} + \frac{\sqrt{2}}{29} + Z_2$$

But $Z_1 = Z_2$ as points (2) and (2) are on the same line and $V_2 = 0$
 $\frac{P_1}{P_0} = \text{pressure head at (1)} = H$
 $\frac{P_2}{P_0} = \text{pressure head at (2)} = (h+H)$.

Substituting these values, we get

 $H + \frac{\sqrt{2}}{29} = (h+H)$
 $h = \frac{\sqrt{2}}{29}$ ore $V_1 = \sqrt{29}h$

This is the prefical invetocity. Actual velocity is given by

 (N) and $= C_1 \sqrt{29}h$

where $C_1 = C_2 \sqrt{29}h$

:. velocity at any point

v= Crvzgh

3 CHAPTER -05 ORIFICE

Introduction ?

Orelifice is a small opening of any cross-section (such as cineular the angular exceedingular etc.) on the side on at the bottom of a tank, through which a bluid is blowing. A mouth piece is a short length of a pape which is two one to three times its diameter in length, kitted in a tank on vessel containing the bluid. Draffices as well as mouth preces are used for measuring the rade of flow , of bluid.

Classification of Driftices >

The onlitices one classified on the basis of their size, shape, nature of discharge and shape of the upsteam edge. The tollowing are the important classifications:-

- (1) The onlyices one classified as small orders on large onlyice depending upon the size of onlifice and head of liquid from the Centre of the orapice. It the head of liquid from the centre of trifice is more than tive times the depth of priffice, the orifice is called small onlyfice. And it the head of liquids is less than five times the depth of prefice, it is known as large online.
- 2) The orifices one classified as (i) Cincular orifice,
 - (ii) Tritangulare onifice (iii) Rectangulare onifice and
 - tivi Square profice depending upon their Cross-sectional arreas
- 3) The onlifees one classified as (1) shortprediged onlifee and a (ii) Bell-mouthed onifice depending upon the shape of cupstream edge of the onligitus.

(4) the orabices are classified as

(i) Free discharging orifices and (ii) Drawned on sub-mercyed correspond to nothing upon the nothing of discharge.

The submerged orifices one burther chustised as (a) fully submerged orifices and (b) partially submerged orifices.

Flow through an Onifice of Consider a tank bitted with a circular onlyice in one ist its eides as shown in bigune.

Let the the head of the liquid subove the centre of the omitice. The liquid whose the liquid blooding through the original borons a jet of liquid whose area of cross-section is less than that of original the area of jet of bluid gloss on decreasing and at a section &-C, the area is minimum. This section is approximately at a distance of half of minimum. This section is approximately at a distance of half of diameter of the original to each other and perpendicular to the straight and portalled to each other and perpendicular to the plane of the original. This section is called Vena-Contracta. Beyond this section, the jet diverges and is attracted in the downward direction by the gravity.

Consider two points I and 2 as showing in bigure. Point I is inside the tank and point 2 at the Vena-Contracta, Let the blow is steady and at a Constant head H. Applying Bernoutile equation at point.

Jet of blund

(Tank with an onitice)

But
$$\frac{P_1}{\sqrt{g}} + \frac{V_1^2}{2g} + Z_1 = \frac{P_2}{\sqrt{g}} + \frac{V_2^2}{2g} + Z_2$$

$$\frac{P_1}{fg} + \frac{V_1^2}{2g} = \frac{P_2}{fg} + \frac{V_2^2}{2g}$$

Vi is very small in comparison to ve as area of tank is very large as compared to the area of the Set of liquid.

This is theoretical velocity. Actual Velocity will be less than this value.

HYDRAULIC CO-EFFICIENTS >

The hydraulic co-applicants are 1-

1] Co-abbicient of velocity, ev

2] co-efficient of Contraction, Ce

3) Co-efficient of discharge, Co

(4) Co-efficient of Velocity (Cv):-

It is defined as the nation between the actual velocity of a set of liquid at vena-Contracta and the theoretical of set.

Out is denoted by Evi and mouthematically inch is given as

Cv = Actual relocity of set at venar contracta.

Theoretical velocity

= vagit , where V= actual velocity, vaget = Theoretical velocity

The value of Co varies brown 0.95 to orga for different orifices, depending on the shape, size of the Orifice and on the head under which blow takes place. Generally, the value of Co=0.98 is taken for sharp-redged orifices.

(2) Co-efficient of Contraction (Cc):-

It is defined as the reaction of the carea of the jet at vena - Contracta to the area of the brifice. It is denoted by Co.

Let a = area of briffice rand

ac = area of Jet at Vena-Contracta

area of Jet at vena-Contracta

area of Driffice

area of Driffice

The value of Co varies from 0.61 to 0.69 depending for shape and size of the oratice and head of liquid under which flow takes place . In general the value of Co may be taken as 0.64.

(3) Co-efficient of Discharge (Cd):-

It is defined as the receipt of the actual discharge trum an orcifice to the theoretical discharge from the orcifice. It is denoted by Cd. It @ actual discharge and Qth is the theoretical discharge then mathematically, Cd is given by Cd = Q - Actual velocity x Actual Area

Cd = Q - Actual velocity x Theoretical area

- Actual velocity x Actual Area

Theoretical velocity Theoretical area

Theoretical velocity Theoretical area

the value of Col variety from 0.61 to 0.65. For general purpose the value of Col is decken as 0.62.

NOTCH

Introduction :-

A notch is a device used for measuring the reade of flow of a higher through a small channel on a tank. It may be defined as an opening in the side of a tank or a small channel in such a really that the liquid surface in the tank or channel is below the top edge of the opening.

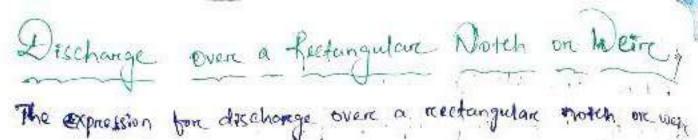
A wein is a Concrete on maionary structure, placed in an open channel over which the flow occurs. It is generally in the form of verdical wall, with a sharp edge cut the top, running all the way across the open channel. The notch is of small size while the wein is of a bigger size. The notch is of small size while the wein is of a bigger size. The notch is generally made of metallic plate while wein is made of Concrete or masonary structure.

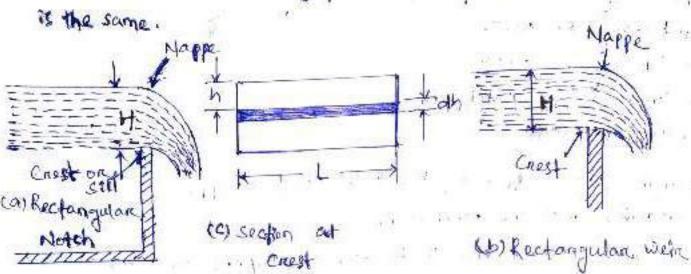
1. Nexpec on Vein: - The sheet of water flowing through a notch

2. Chest on the bottom edge of a notch on a top of a weign over whach the wester flows, is known as the Classification of Notes and weires ?

The notches aree classified as :

- (1) According to the shape of the opening:
 - (a) Rectangular notch
 - (b) Trixingulare notch
 - (c) Trapozordal noteh and-
 - (d) stepped notch
- (2) According to the effect of the sides on the nappe:
 - cas Notch with end contraction
 - (b) Notch without end contraction on suppressed notch
 Weine are classified according to the shape of the opening, the
 shape of the Creek, the about of the side on the nappe and
 nature of discharge. The following are important classification.
 - (a) According to the shripe of the opening:
 - (i) Rectangular wein
 - (18) Tritangulare were and
 - (in) Thapezordal wein (Cipalletti wein)
 - (b) According to the shape of the crest:
 - (1) Sharp-enosted wellow
 - (15) Broad-Crested weir
 - (ti) Nannow-Crested wein and
 - (14) Dejae Shaped wetre
 - (c) According to the effect one sides on the emerging nappe;
 - (i) Well with end contraction and (i) Well without end





(Rectangulare notch and weire)

Consider a rectangular notch on we're provided in a channel carrifing water as shown in figure.

Lef H= Head of water over the court
L= Length of the notch on work

For finding the discharge of water flowing over the wein on noth, consider an elementary horizontal estrop of water of thickness of and length L at depth h from the free & surface of water is shown in begune.

The area of strip = Lxdh

and theoretical velocity of water blowing through strip = Vagh

The discharge de, through strip is

de = Cd x Area of strip x Theoretical Velocity

= CyxLx dhx vzgh

where Col = co-efficient of abschange

rihe total discharage. Or, for the whole noteh on wein is defermined by integrating equation (i) between the limits 'D and H . :. Q = 5th Carl. 129h dh = CAXLX VZg St hV2dh = Cax Lx/2g [h/2+1] = CdxLx \sq \[\frac{h^{3/2}}{3/2} \] H = 3 Cox LX (29[H]3/2 Vischange Over a Triangular Notch on Weire of The expression for the discharge over a triangular notth on we fin is the same. It is the derived as: Let H = head of water above the V-notch O= angle of notch . Consider a horizontal strip of water of threeness did at a depth of h from the bree surface of water as shown in figure. Box September . from figure (b), we have tan = AC = AC· AC = (H-h) tan 0 width to strip = AB = 2AC = 2 (H-h) tan 0/2 As

: Accord strip = 2(4-h) fan 0/2 x dh

The theoretical velocity of water through strop = 29h

Discharge, through the strop,

de = Cox Area of strop x velocity (theoretical)

= Cd x a(H-h) tan 0/2 x dh x vegh

= 20d B(H-h) tan 0/2 x 29h x dh

Total discharge,

Q = Stronge,

Q = Stronge,

Q = Stronge,

Area of strop x velocity (theoretical)

= 20d K tan 0/2 x 29f (H-h) h vegh

= 20d K tan 0/2 x 29f (H-h) h vegh

= 2x cd x tan 0/2 x 29 ft (H-h) h vegh

= 2x cd x tan 0/2 x 29 ft (H-h) h vegh

= 2x cd x tan 0/2 x 29 ft (H-h) h vegh

= 2x cd x tan 0/2 x 29 ft (H-h) h vegh

= 2x cd x tan 0/2 x 29 ft (H-h) h vegh

= 2x cd x tan 0/2 x 29 ft (H-h) h vegh

= 2x cd x tan 0/2 x 29 ft (H-h) h vegh

= 2x cd x tan 0/2 x 29 ft (H-h) h vegh

= 2x cd x tan 0/2 x 29 ft (H-h) h vegh

= 2x cd x tan 0/2 x 29 ft (H-h) h vegh

= 2x cd x tan 0/2 x 29 ft (H-h) h vegh

= 2x Cd X tan 9/2 x \(\begin{array}{c} \frac{2}{3} \text{H} \text{H}^{3/2} - \frac{2}{5} \text{H}^{5/2} \]

= 2x Cd X tan 9/2 x \(\begin{array}{c} \frac{2}{3} \text{H}^{5/2} \]

= 2x Cd X \text{tan 9/2 x \(\begin{array}{c} \frac{2}{3} \text{H}^{5/2} \]

= 2x Cd X \text{tan 19/2 x \(\begin{array}{c} \frac{4}{15} \text{H}^{5/2} \]

= \frac{8}{15} Cd X \text{tan 9/2 x \(\begin{array}{c} \frac{4}{3} \text{H}^{5/2} \]

= \frac{8}{15} Cd X \text{tan 9/2 x \(\begin{array}{c} \frac{4}{3} \text{H}^{5/2} \]

For a right angled V-notch if $C_d = 0.6$ $0 = 90^\circ$, i.tan 0/2 = 1

Discharge, Q = 8 x 0.6 x 1 x \2x9.81 x H5/2 = 1.417 H5/2

Loss of Energy in pipes ?

When a bluid the blowing through a pipe, the bluid expendences some resistance due to which some of the energy of bluid is lest. This loss of energy is classified as:

Energy losses

1

This is due to brickion and it is calculated by the bollowing formulae 1

formulae:
(a) Dancy- weis bach formula (c) Bond in pipe

LMajor Energy losses . . . 2 Minon Energy losses

This is due to (a) Sudden expansion

(b) Sudden Contraction

. .

LOSS OF Energy (OR HEAD) DUE TO FRICTION &

19) Dancy - Wessbach Foremula :-

The loss of head (on energy) in purpose pipes due to furction is calculated brom Dancy-weisbach equation which has been derived in chaptere to and is given by $h = 4.5 \cdot L \cdot V^2$

 $h_{\xi} = \frac{4. \, \xi \cdot L \cdot V^2}{91 \times 29}$

where he = 1035 ob head due to briction,

by = co. afficient of bruction which is a function of, Reynold's number.

= 16 for Re W 2000 (VOSCOUS Blow).

= 114 for Re Varying from 4000 to 106 L = length of pipe V = mean velocity of blow d = doameter of pape (b) Chezy's Foremula fore loss of head due to bruietion in pipes: Retent to Chapter to auticle to in which expression born loss of head due to britation in people pipes is derived. . Equation (187) of audicle to ho F to x P x LX V2 where he = loss of head due to batchion -P = welted personeten of fire A = Area of crease-section of pipe 1. Lastength of Pope V= mean velocity of blow Now the realto of P (Area of blow) is called hydrauly mean depth on hydroulic reading and is denoted by m. tydraudic mean depth, m = A = 30 = d Substituting . A = m on P = in equation (2), we get. ht = by x Lx v2x from v2 = htx fg xmx & L The state of Seap 2 = fg xmxhb JA L (FLXWX WE. = 1 13 (3). Let 19 = c, where c is a constant known as chezy's constant and the = i, where is is loss of shead per unit length of pope substituting the values of very and to in equation = (3)
we get . V = Cvmi . - (4).

regulation. (4) is known as Cherry's borimula. Thus the loss of head due to briction on a in pipe broom cherry's borimula can be obtained it the velocity of blow through pipe and also the value of C is known. The value of m for pipe is always equal to other of 4.

MINIOR ENERGY (HEAD) LOSSES 7

The toss of head on energy due to traction in a prope is known as major toss while the loss of energy, due to change of velocity of the bollowing bluid in magnitude on direction is called minor boss of energy. The minor toss of energy (or head) includes the bollowing cases:

- 1. Loss of head due to sudden enlargement,
- 2. Loss of head due to Sudden conficaction,
- 3. Loss of head stacks at the entrance of a pipe.
- 4. Loss of head out the exit of a pipe
- 5. Loss of head due to an obstruction in a pipe,
- 6. Loss of head alue to bend in the pipe.
- 7. Loss of head in Marrious pipe bittings.

In case of long pape the above losses are small as compared with the loss of head due to briction and hence they are called minor losses and even may be neglected without serious error. But in case of a short pape, these losses are comparable with the loss of head due to friction.

HYDRAULIC GRADIENT AND TOTAL ENERGY LINE ?

The concept of hydroculic greatient line and total energy line is very useful in the study of the blow of blueds through pipe. They are defined as:

Hydraulic Gradient Line ?

It is defined as the line which gives the sum of pressure. Adad (P) and datum head (Z) of a flowing bluid in a pope with respect to some reference line on it is the line which is obtained by Joining the top of all ventical ordinates, showing the pressure headleplus) of a flowing bluid in a pipe from the centre of the pipe. It is briefly written, as they. Chydraulic (gradient line).

Total Energy Line 7

It is defined as the time which gives the sum of pressure head obtained and kinetic head of a blowing blund in a pipe with respect to some reference line. It is also defined as as the line which is obtained by soining the tops of all verdical ordinates showing the sum of pressure head and kinetic head from the Centre of the pipe.

It is briefly written as T.E.L. (Total Energy Line).

Introduction 7

The loquid comes out in the bound of a Jet broom the outlet 'Of a nozzle, which is the bitted to a pipe through which , the thirt liquid is blowing under pressure. It some plate, which may be fixed on moving, is placed in the path of the Jet, a force is exercted by the Jet on the plate. This bonce is obtained from Newton's 2nd law of motion or from impulse-momentum equation. Thus impact of Jet means the force exerted by the jet on a plate which may be stationary or moving. In this Chapter, the following cases of the impact of jet ine. the force exercted by the jet on a plate, will be considered.

3

- (1) Force exerted by the set on a stationary plate when (a) place is viertical to jet
 - (b) plate is inclined to the jet, and
 - (c) plate is curved.
- (a) Place exercted by the set on a moving place, when

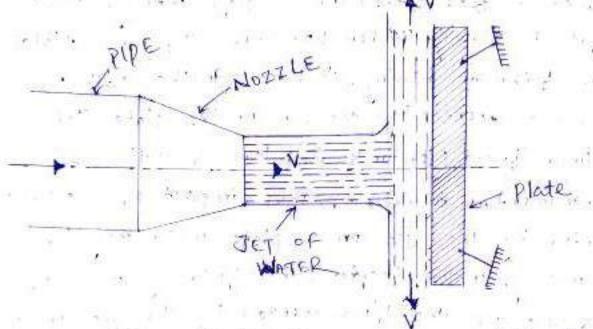
And the state of t

the form the first product of the second

- (a) place is ventical to viet,
- (b) plate is inclined to the Jet and
 - (c) plate is curved.

Force Exerded By The Jet On a stationary Ventical Plate 7

Gonsider a Jet of water coming out from the nozzle, strukes a blat vertical plate as shown in the below figure.



(Force exerded by set on ventical plate)

Let V = velocity of the jet

de diameter of the jet

a = anea of chois section of the Jet = # 92

The Jet abten straining the plate, will move along the plate:

But the plate is at right angles to the jet.

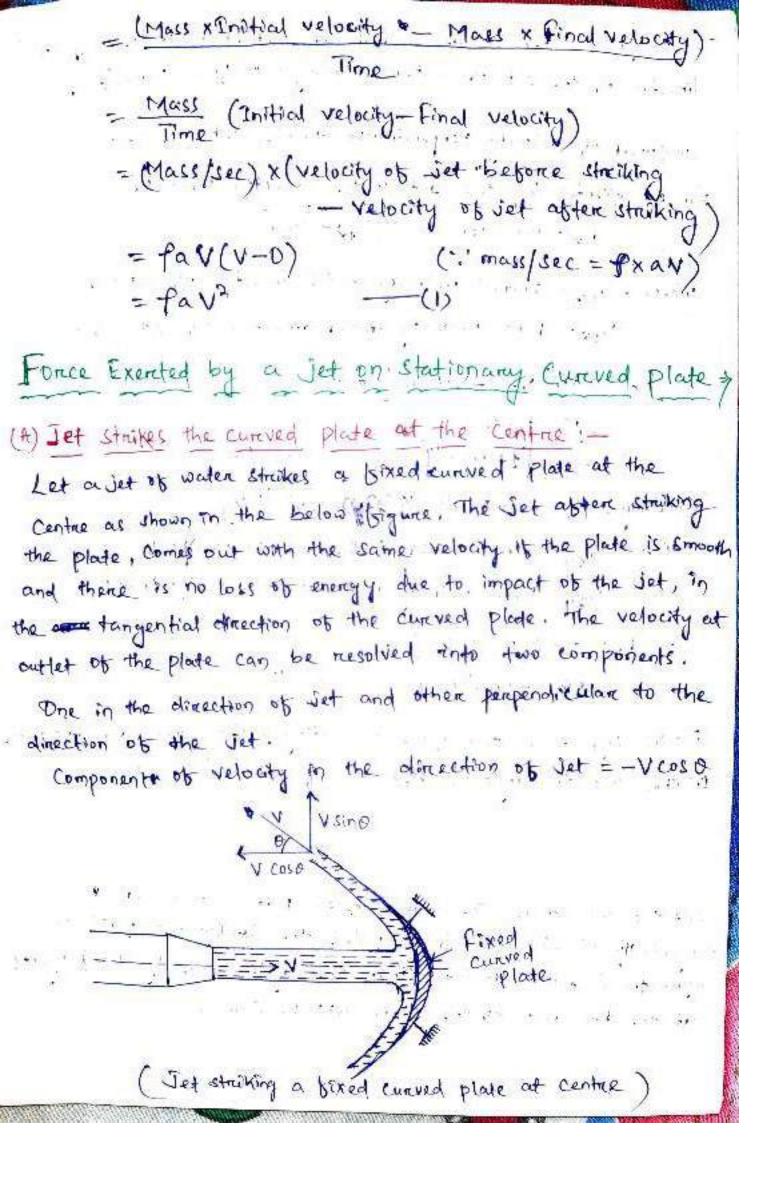
Hence the jet abten A Straining, will get deflected through 90° Hence the Component of the velocity of jet in the direction of Jet, after straining will be zero.

The bonce exercted by the set on the plate in the direction of set.

Fx = Rate of change of momentum in the direction of force

Initial momentum - Final momentum

Time



(-ve sign is taken as the velocity at outlet is in the opposite direction of the set of water coming out from Nozzle).

Component of velocity perpendicular to the jet = $V \cos \theta$. Forced exerted by the jet in the direction of jet, $F_X = moss per sec \times [V_{1X} - V_{2X}]$

where, $V_{2X} = 2nitical$ relocity in the direction of Jet = V $V_{2X} = Final$ relocity in the direction of Jet = -V cos a

-- Fav[v-(-v(0))] = = fav[v+v(0)] = = fav[v+v(0)] = - (3)

Simplainly, Fy = mass part sec x 2 V2y - V2y]

values, $V_{xy} = Enitial valuesty in the direction of <math>y = D$. $V_{xy} = Final valuesty in the direction of <math>y = V \sin Q$.

 $F_{y} = f_{a}v_{0} - v_{sino}$ $F_{y} = f_{a}v_{sino}$ - (3)

2 - Ve sign means that borce is acting in the downward director. In this case the angle of deflection of vet = (150 - 0)

(B) Jet Strikes the Curved plate out one end tangentially when the plate is symmetrical;

Let the Jet Striker the Curved bixed plate at one end & tangentially as shown in tigare. Let the concurred plate is symmetrical about straxis. Then the angle made by the trangents at the two ends of the plate will be some.

Let V= relocity of jet of water

&= Angle made by jet with makes

at inlet tip of the curved plate

If the Plate is smooth and loss

of energy due to impact is Zeno,

then the velocity of water & at the

outlet tip of the curved plate will be

equal to V. The forces exerted by the

Jet of water in the dimensions of

a and y are

Fx = (mass/sec) x [Vix - Vax]

= fa V [Vcoso - (-Vcoso)]

 $F_{X} = (\max | sec) \times [V_{1x} - V_{2x}]$ $= fa V [V \cos o - (-V \cos o)]$ $= fa V [V \cos o + V \cos o]$ $= 2fa V^{2} \cos o - (4)$

Fy = fav [Viy-Vay]
= fav [vina - vina] = 0

Jet stroking Curved bixed plate out one end

T VSIN 0

(C) Jet strikes the Curved plate at one end tangentially when the plate is unsymmetrical:

When the curved plate is unsymmetrical about X-axis, then angle made by the tangents drawn at the inlet and outlet tips of the plate with 1x-axis, will be alitherent.

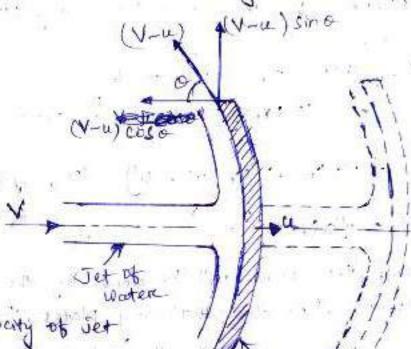
Let = angle made by tangent at outle't tip with X-axis.

The two components of the velocity cut inlet core

Vix = V cos B and .Viy = Vsin Q.

Force on the Cureved Plate when the plate is moving in

Let a jet of water strukes a Curved plate at, the Centre of the plate which is moving with a uniform velocity in the direction of the viet as shown in the figure.



Ket V = Absolute velocity of Jet

a = onea of Jet

u = velocity of the plate ! !

in the direction of the viet

- curryed.

Jet straking a Curved moving

The velocity with which jet strikes the curved plate = (V-u).

- It place is smooth and the loss of energy due to impact to jet is Zeno, then the velocity with which the jet will be too leaving the Curved Vane = (V-u).
- This velocity can be restored into two components, one in the direction of the Jet and other perpendicular to the direction of the Jet

component of the velocity in the direction of ordet = - (V-u) cosa

(ve sign is taken as at the outlet, the component is in the opposite direction of the vet).

component of the velocity in the alinection perspendicular to the direction of the Jet = (V-u) sin a

Mass of the water struking the plate

= fx a x velocity with which jet strukes the plate

= fxa(V-u).

: Fonce exemped by the Jet of water on the curved plate in the direction of the Jet,

Fx = mass stricking pensec X [Enitial velocity with which wet strickes the place in the direction of wet - Final velocity]

= fa (v-u) [(v-u) + (v-u) cos o]

= fa (v-u)2 [1+ cos 0] . - (9)

Workdone by the set on the plate per second

= Fx x Distance travelled per second in the direction

the state of the s

 $=F_X \times u$

= $fa(v-u)^2[1+\cos \sigma]u$

= Pa (v-w)2 x u [1+cose] - (10)

A PART OF THE PART

the complementary was a series of the complementary was a series of

Force Exercted by a Jet of Water on an Unsymmetrically Moving curved plate on when Jet strukes Tangentially

The above figure shows a jet of water struking a moving curved plate (also called vane) tangentially, at one of its tips. As the jet strukes tangentially, the loss of energy due to impact of the jet will be zero. In this case as plate is moving the velocity with which jet of water strukes is equal to the relative velocity of the jet with respect to the plate. Also as the plate is moving in different direction of the jet, the relative velocity of will be equal to the western object or difference of the velocity of will be equal to the western objects and velocity of the plate at inlet.

Let $V_1 = Velocity of the viet at inlet

[u_1 = Velocity of the plate (Vane) at inlet

Vr.s = Relative velocity of viet and plate at inlet$

of motion of the plate, also called guide blade angle

D = Angle made by the relative velocity ("Virg) with the direction of motion at inlet also called Name angle at inlet

View and Vig = The components of the velocity of the jet V1, in the direction of motion and perspendicular to the direction of motion of the Vane respectively.

VW1 = It is also known as velocity of whire out inlet

Vo1 = It is also known as velocity of blow at inlet

V2 = velocity of the list, leaving the vane on velocity of list

at outlet of the vane.

lez = Nelocity of the Vane at outlet

Vrz = Relative velocity of Jet with respect to the vane at outlet

B = Angle made by the vetocity V2 with the direction of the vane at outlest.

\$\phi = Angle made by the relative velocity (Vaz) with the direction of motion of the Vane of Dutlet and also be called vane angle at Dutlet

Vwa and Vta = Components of the velocity Vz, in the direction of motion of vane and perpendicular to the direction of motion of vane at outlet

Vwa = It is also called the velocity of whire at outlet

'Vrz = Velocity of 61000 at outlet

The tricingles ABD and EGH are called the velocity tricingles at inlet and outlet. These velocity triangles are drawn as given below:

(1) Velocity Trainigle at Inlet;

Take any point of and draw a line AB = 4 in # magnitude and direction which means line AB makes an angle or with the horizontal line AD. Next draw a line AC = 4 in magnitude. Join C to B. Then CB represents the relative velocity of the vet at inlet. It the loss als renergy out inlet due to impact is zero, then CB must be in the tangential direction to the vane at inlet. From B draw a ventical line BD in the down warred direction to meet the horizontal aline AC produced out D.

Then BD = Represents the velocity of blow out inlet = Vs1

AD = Represents the velocity of whird out inlet = Vish

LBCD = Vane single at inlet = D

LBAC = X

(3) Velocity Triangle at Outlet: -

The the vane Surveyace is assumed to be very smooth, the loss of energy due to braction will be zero. The water with be gliding and over the Surveyace of the vane with a relative velocity equal to Vas and will come out of the vane with a relative velocity very very this means that the relative velocity at outlet Vaz = Vas.

And also the relative velocity at outlet should be in tangential direction to the vane at outlet.

Draw Ely in the turgential direction of the Vane at outlest and out Ely = Vaz.

from 6, draw a line Gift in the direction of vone at outlet and equal 40 uz, the velocity of the Vane at outlet.

Join EF, then EF represents the absolute velocity of the jet at outlet in magnitude and direction. From Edinar a vertical line EH to meet the line 4F produced at H.

Then EH = velocity of blow cet but let = Vb2.

FH = velocity of whird at outlet = Vw2

LEGF=Φ = Angle of the Vane at our let

LEGF=B = Angle made by V2 with the direction of motion of

Verne cot outlet.

If the vane is smooth and is having velocity in the direction of motion at inlet and outled equal then we have

u = uz = u = - velocity of vane! in the direction of

and Vry= Vrez.

Whene a = Anea of Jet of water

Vr. = Relative velocity at inlet

. Fonce exerted by withe Jet in the direction of motion

Fx=mass of worden striking per sec X

Enother velocity with respect to which jet stribles in the direction of motion — Fond velocity of in the direction of motion]

But instead velocity with which set the struckes the vane = Vica .

The component of this velocity in the direction of motion = Vica cosp = (Viv. - u1)

Similarly, the components of the relative velocity at outlet in with a direction of motion = - Vac los of =- [u2+Vw2] - We sign is taken as the component of Vaz in the direction of motion is in the opposite direction. Substituting the equation (1) and all above values of the velocities in equation (2), we get Fx = Pavil ((Vo) + in) - = {-(u2+ Vo2)} = favr, [Vw1 - u1 + u2 + Vw2] = favry [Vw1+Vw2] . (: 4 = 42) . - (3)) Equation (3) is true only when angle 13 shown in bigune is an acute angle. It B= 90°, the Vwz = D, then equation (3) becomes as, Fx = fa Vr. [Vwi] It Bis an obtuse angle, the expression bon Fx will become Fx = Pa Vry [WW Vwj - Vwz] Thus in general, Fx 25 written as Fx = falke, [Vw/t Vw2] Work done pen second on the vone by the jet

= Force & Distance per second in the direction of force = Fx x u

= Paka[Vwit Voz] Xu

. Workdone pen second pen unit weight of bluid striking pen second = faxx, [Vw, + Vwz] xu Nmls NIS weight of bluid striking Is

= faver [Vw1+ Vw2] xu No gx Pava

= \frac{1}{9} [Vw1 \pm Vw2] \times \times \text{Nm/N} \quad -(5)

Work done [see per unit mass of bluid stroking per second

= \frac{1}{2} Vw1 \pm Vw2] \times \text{Nm/s}

Favor | \frac{1}{2} Vw2] \times \text{Nm/s}

= \frac{1}{2} Vw1 \times Vw2] \times \text{Nm/s}

= \frac{1}{2} Vw1 \times Vw2] \times \text{Nm/kg}

= \frac{1}{2} Vw1 \times Vw2 \times \times \text{Nm/kg}

(3) Efficiency of JET ?

The work done by the Jet on the vane given by equation (4) is the foutput of the Jet where as the initial kinetic energy of the Jet is the input. Hence, the effectionary (91) of the Jet is expressed as

91 = Dutput = Workdone per second on the Vaine
Intral Kinetic Energy per second of the Set

= fa Vr. (Vw. + Vw2) x u

1/2 m V.2

Where m = mass of the bluid per second in the jet = fav, V, = invitial velocity of Set

:. 91 = fa Vry [Vw1 ± Vw2] xu ___ (7)

MODEL SET QUESTION PAPER FOR PRACTICE SET-1 Semester: 4th Branch: Mechanical Engineering Subject Name: Fluid Mechanics Full Marks- 80 Time- 3 Hrs Answer any five Questions including Q No.1& 2 Figures in the right hand margin indicates marks

1.		Answer All questions	2 x 10
	a.	Define Mass Density. What is its unit?	
	b.	Define the term Kinematic Viscosity. State its SI unit.	
	c.	State Archimede's Principle.	
	d.	What do you mean by Surface Tension? State the expression for Surface	
		Tension on a hollow bubble.	
	e.	What is mean by Vaccum pressure and Atmospheric pressure?	
	f.	Define Buoyancy.	
	g.	What do you mean by Metacentre?	
	h.	Define uniform and non-uniform flow.	
	i.	Define Pitot Tube.	
	j.	What is meant by Total Energy Line?	
2.		Answer Any Six Questions	5 x 6
	a.	Derive the expression for Capillarity Fall.	
	b.	Derive the expression for rate of flow through venturimeter.	
	c.	Classify Notch into its different categories.	
	d.	What are the Different Losses of energy in pipes? State the Darcy Weisbach Formula for head loss.	
	e.	The diameter of a pipe at the section 1 and 2 are 10cm and 15cm respectively. Find the discharge through the pipe if the velocity of water flowing through the pipe at section 1 is 5cm. Find the velocity at section 2.	
	f.	A plate 0.025mm distant from a fixed plate, moves at 60cm/s and requires a force of 2N/m ² to maintain this speed. Determine the viscosity of fluid between the plates.	
	g.	Write a short note on "Differential Manometers"	
3		Derive the force exerted by a jet in the direction of the jet on a moving	10
		unsymmetric curved plate when the jet strikes tangentially at one end of the	
		plate. Also derive the work done per second on the plate.	
4		Define Orifice. Derive the expression for flow through orifice. A sharp edged	10
		orifice of 5cm diameter discharges water under a head of 4.5m. Determine the	
		coefficient of discharge if the measured rate of flow is 0.0122m ³ /s.	

5	State and derive the Bernoulli's theorem for steady flow for an incompressible	10
	fluid. What are the assumptions made in the derivation of Bernoulli's equation?	
6	A rectangular plane surface is 2m wide and 3m deep. It lies in vertical plane in	10
	water. Determine the total pressure and position of center of pressure on the	
	plane surface when its upper edge is horizontal and	
	I. Coincides with the water surface.	
	II. 2.5m below the free water surface.	
7	A jet of water 40mm diameter moving with a velocity of 120m/s impinging on	10
	a series of vanes moving with a velocity of 5m/s. Find the force exerted,	
	workdone and efficiency.	

MODEL SET QUESTION PAPER FOR PRACTICE SET-2 Semester:4th Branch:Mechanical Engineering Subject Name: Fluid Mechanics Full Marks-80 Time-3 Hrs Answer any five Questions including Q No.1& 2 Figures in the right hand margin indicates marks

1.		Answer All questions	2 x 10
	a.	Define Weight Density. What is its unit?	
	b.	What do you understand by Continuity Equation?	
	c.	What do you mean by Capillarity?	
	d.	What do you mean by Surface Tension? State the expression for Surface	
		Tension on a liquid jet.	
	e.	What is mean by Absolute pressure and Gauge pressure?	
	f.	What are the assumptions made in the derivation of Bernoulli's equation?	
	g.	What do you mean by Metacentric Height?	
	h.	Define steady and unsteady flow.	
	i.	Define Orifice.	
	j.	What is meant by Hydraulic Gradient Line?	
2.		Answer Any Six Questions	5 x 6
	a.	Derive the expression for Capillarity Rise.	
	b.	Derive the pressure expression for a inverted differential U-Tube Manometer.	
	c.	Define Pitot tube. Derive the expression of velocity at a point using Pitot Tube.	
	d.	Derive the discharge over a Rectangular Notch.	
	e.	What are the guage pressure and absolute pressureat a point 3m below the free	
		surface of a liquid having a density of 1.53×10 ³ kg/m ³ . Given that the	
		atmospheric pressue is 750mm of mercury, the specific gravity of mercury is	
		13.6 and density of water is 1000 kg/m ³ .	
	f.	A solid cylinder of diameter 4m has a height of 3m. Find the metacentric height	
		of the cylinder when it is floating in water with its axis vertical. The specific	
		gravity of the cylinder is 0.6.	
	g.	State and derive the Pascal's Law.	
3		Derive the following for a moving unsymmetric curved plate when the jet	10
		strikes tangentially at one end of the plate:	
		I. force exerted by a jet in the direction of the jet.	
		II. work done per second per unit weight of fluid on the plate.	
		III. Efficiency of the jet.	

4	State the Darcy Weisbach Formula and Chezy's Formula for loss of head.	10
	Water flows through a pipe of 200mm in diameter and 60m long with a	
	velocity of 2.5m/s. find the head loss due to friction using:	
	I. Darcy's formula where $f = 0.005$	
	II. Chezy's formula where $c = 55$	
5	An oil of specific gravity 0.7 is flowing through a pipe of diameter 300mm at	10
	the late of 500l/s. find the head loss due to friction and power required to	
	maintain the flow foe a length of 1000m. Take kinematic viscocity as 0.29	
	stroke	
6	A pipeline, 300mm in diameter and 3200m long is used to pump up 50 kg/s of	10
	an oil whose density is 950 kg/m ³ and whose kinematic viscosity is 2.1 stokes.	
	The centre of the pipeline at the upper end is 40m above than that at the lower	
	end. The discharge at the upper end is atmospheric. Find the pressure at the	
	lower end and draw the hydraulic gradient line (HGL) and the total energy line	
	(TEL).	
7	State and derive the Bernoulli's theorem for steady flow for an incompressible	10
	fluid. What are the assumptions made in the derivation of Bernoulli's equation?	

MODEL SET QUESTION PAPER FOR PRACTICE SET-3 Semester:4th Branch:Mechanical Engineering Subject Name: Fluid Mechanics Full Marks-80 Time-3 Hrs Answer any five Questions including Q No.1& 2 Figures in the right hand margin indicates marks

1.		Answer All questions	2 x 10
	a.	Define Specific Gravity. What is its unit?	
	b.	Define the term Dynamic Viscosity. State its SI unit.	
	c.	What is mean by Rate of Flow or Discharge?	
	d.	What do you mean by Surface Tension? State the expression for Surface	
		Tension on a water bubble.	
	e.	State the Bernoulli's theorem for steady flow for an incompressible fluid.	
	f.	Define centre of pressure.	
	g.	What do you mean by Bouyancy?	
	h.	Define Laminar and Turbulent flow.	
	i.	Define Venturimeter.	
	j.	State the Chezy's Formula for loss of head.	
2.		Answer Any Six Questions	5 x 6
	a.	State and derive the Pascal's Law.	
	b.	Classify the Hydraulic Coefficients. State the relationship between them.	
	c.	Derive the discharge over a Traingular Notch.	
	d.	Find the discharge of water flowing over a rectangular notch of 2m length	
		when the constant head over the notch is 300 mm. Take Cd= 0.60.	
	e.	Derive the force exerted by a jet in the direction of the jet on a moving	
		unsymmetric curved plate. Also derive the work done per second on the plate.	
	f.	Calculate the specific weight, specific mass, specific volume and specific	
		gravity of a liquid having a volume of 6m ³ and weight of 44kN.	
	g.	Write a short note on Bourdon Tube Pressure Guage.	
3		I. The head of water over an orifice of diameter 40mm is 10m. find the actual	10
		discharge and actual velocity of jet at vena contracta. Take $C_C = 0.6$ and C_d	
		= 0.98.	
		II. The discharge over a rectangular notch is 0.135 m 3 /s when the water level is	
		22.5m above the still. If the coefficient of discharge is 0.6, find the length	
		of the notch.	
4		I. Describe Hydraulic Gradient Line and Total Energy Line.	10
		II. Derive the continuity equation.	

5	Define Metacenter and Metacentric Height. Derive the expression for	10
	Metacentric Height.	
6	Derive the pressure expression of a simple U-Tube manometer. The right limb of a simple U-tube manometer containing mercury is open to the atmosphere while the left limb is connected to a pipe in which a fluid of specific gravity 0.9 is flowing. The centre of the pipe is 12cm below the level of mercury in the right limb. Find the pressure of fluid in the two limbs if the difference of mercury level in the two limbs is 20cm.	10
7	A jet of water of diamter 10cm strikes a flat plate normally with a velocity of 15m/s. the plate is moving with the velocity of 6m/s in the direction of the jet and away from the jet. Find: I. The force exerted by the jet on the plate. II. Work done by the jet on the plate per second.	10